

University of Stuttgart

Institut für Technische Verbrennung (ITV)

Nanoparticle Agglomeration – towards scale preserving computations

UKCTRF Annual Meeting

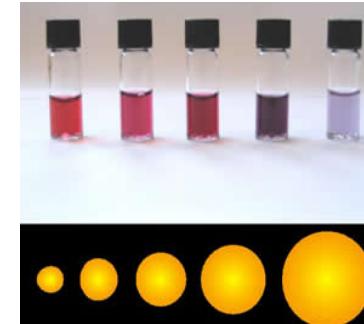
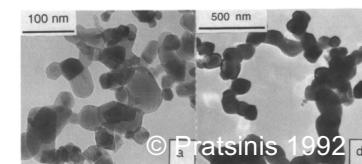
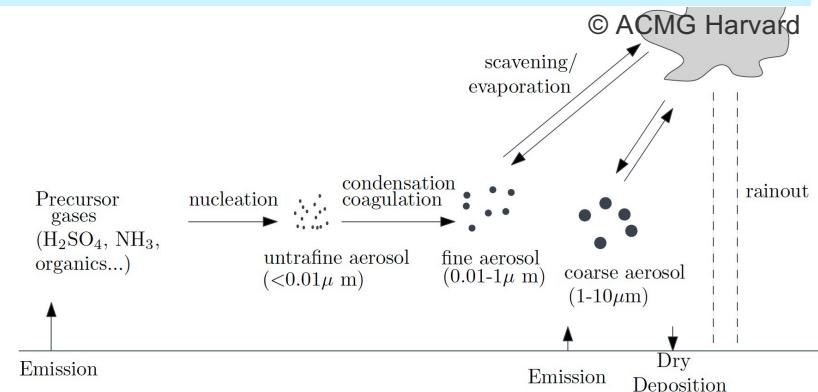
Cambridge – 12th - 13th September 2018

A. Kronenburg, M.
Smiljanic, S.
Hirschmann, D.
Pflüger

Motivation & Outline

Agglomeration

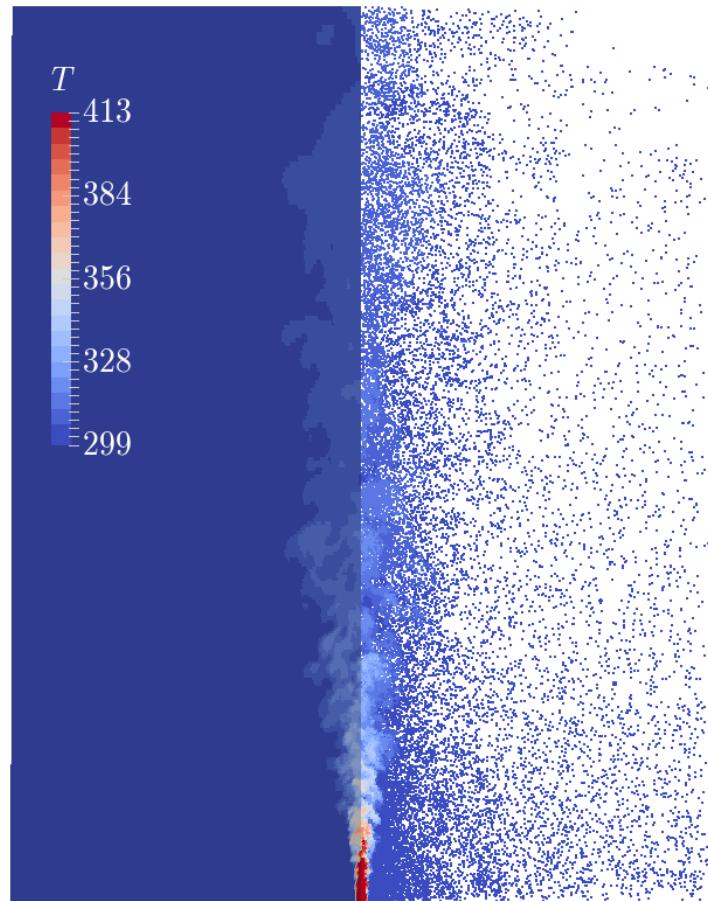
- Importance
 - Environment – aerosol formation
 - Water purification
 - Exhaust treatment
 - Spray drying
 - Particle flame synthesis
- Agglomeration determines size and size determines properties
 - optical/magnetic/electrical/mechanical



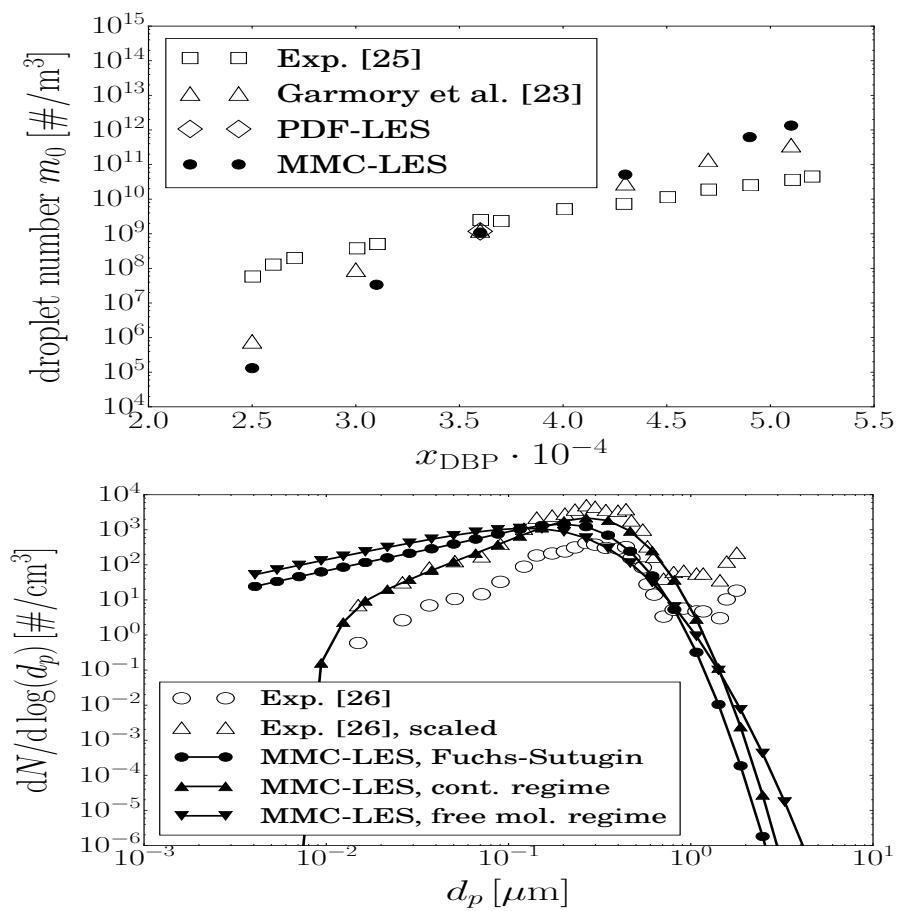
Motivator: Particle Synthesis

Existing PDF-MMC simulations of UCLA experiment (Friedlander)

HOT DBP-LADEN JET IN COLD CO-FLOW



PREDICTED M_0 UND PSD

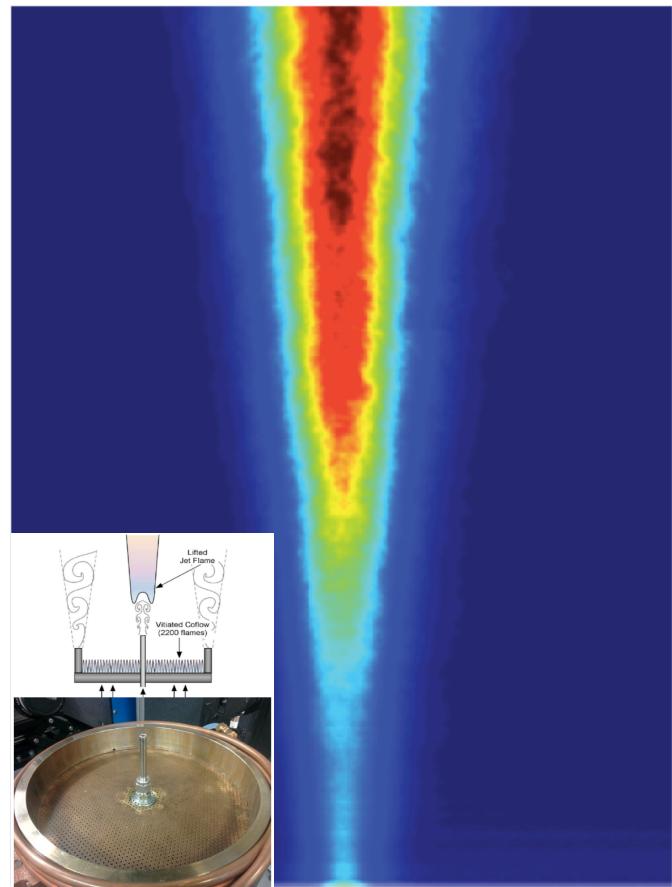


but very dilute and no agglomeration

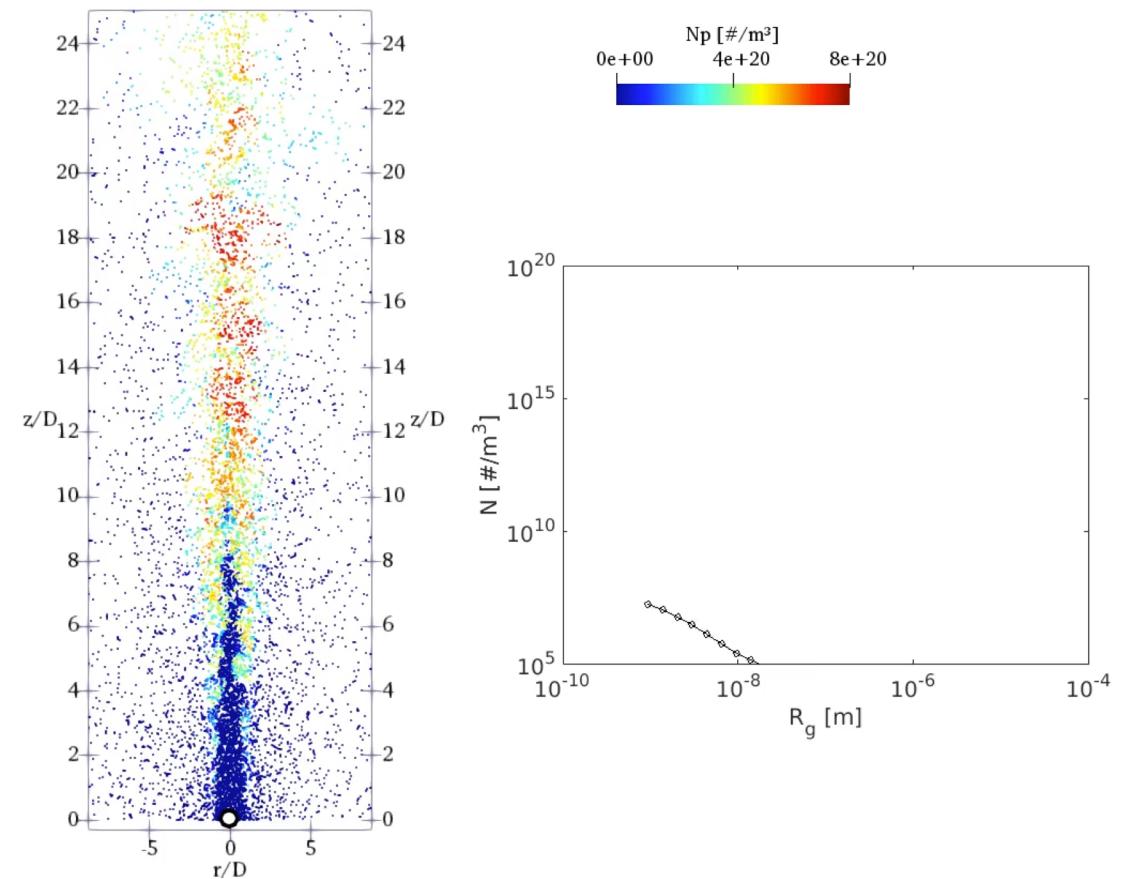
Motivator: Particle Synthesis

Existing PDF-MMC simulations of silica formation

ELASTIC LIGHT SCATTERING SIGNAL



PREDICTED PSD



G. Neuber et al., Proc. Combust. Inst., in press (2019)

Motivation & Outline

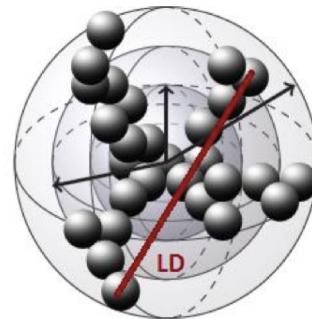
Agglomeration models

- Motivation
 - Turbulence-chemistry interactions
 - Turbulence-particle interactions
 - Particle-particle interactions
 - Existing models do not usually account for
 - Varying morphology of agglomerate during agglomeration process
 - Effects of flow field other than shear
 - Collision frequencies for fractals in turbulence
- Outline of talk
 - Some hypotheses about morphology
 - Parameterization of D_f
 - Supercomputing or coarse-graining approach?
 - Comparison between coarse-graining and detailed Langevin dynamics

Agglomeration

Collision kernel

- The PBE $\frac{\partial n}{\partial t} + \nabla \cdot n \mathbf{u} - \nabla \cdot D \nabla n + \frac{\partial G(v, \mathbf{Y}) n(v)}{\partial v} = S(v, \mathbf{Y}) + \frac{1}{2} \int_0^v \beta(\tilde{v}, v - \tilde{v}) n(\tilde{v}) n(v - \tilde{v}) d\tilde{v} - \int_0^\infty \beta(v, \tilde{v}) n(v) n(\tilde{v}) d\tilde{v}$
- Collision frequency, β , dependent on aggregate's shape
- Use fractal dimension D_f to characterize shape



$$N = k_f \left(\frac{R_g}{\sigma / 2} \right)^{D_f}$$



Free molecule regime



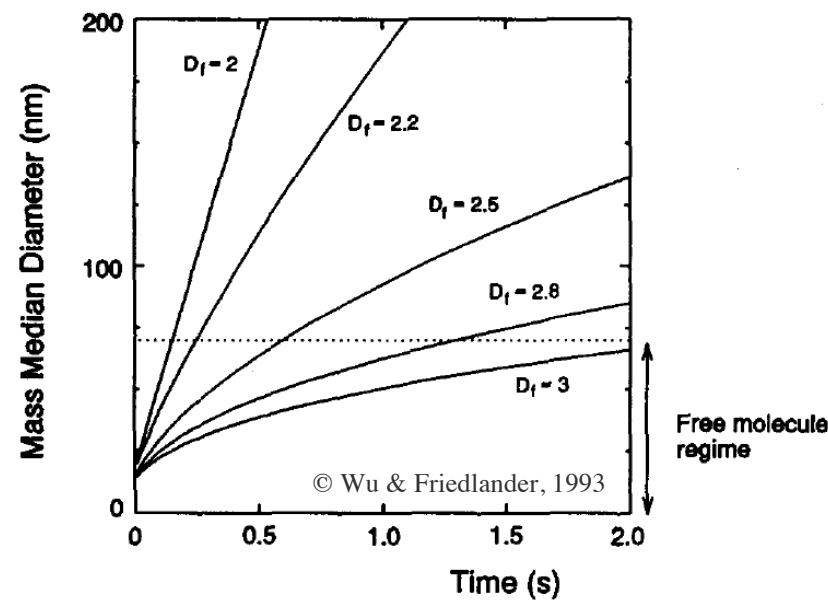
Continuum regime

$$\beta(v_i, v_j) = \left(\frac{6k_b T}{\rho} \right)^{1/2} \left(\frac{3}{4\pi} \right)^{2/D_f - 1/2} d_{p0}^{2-6/D_f} \left(\frac{1}{v_i} + \frac{1}{v_j} \right)^{1/2} \left(v_i^{1/D_f} + v_j^{1/D_f} \right)^2$$
$$\beta(v_i, v_j) = \frac{2k_b T}{3\mu} \left(\frac{1}{v_i^{1/D_f}} + \frac{1}{v_j^{1/D_f}} \right) \left(v_i^{1/D_f} + v_j^{1/D_f} \right)^2$$

Agglomeration

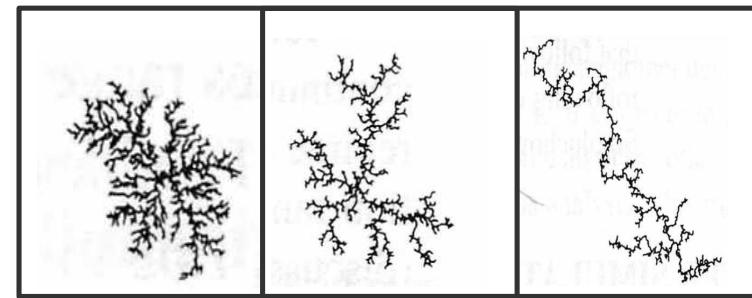
The fractal dimension D_f

IS D_f IMPORTANT?



WHAT IS D_f ?

- Hypothesis 1: D_f affected by turbulence.



© Meakin, 1988

- Hypothesis 2: D_f is no function of time.

Agglomeration

How to determine D_f ?

- The motion and dynamics of the Brownian particles are modelled by solving the Langevin equations of motion

$$m_P \ddot{\mathbf{x}}_i = F_D + F_{ext} + BdW$$

$$\dot{\mathbf{x}} = \mathbf{v}(t, x)$$

- Use ESPreSo 
 - Molecular dynamics package
 - Attractive-repulsive L-J force

$$U_{LJ}^{attractive}(r) = -\frac{A}{6} \left[\ln\left(\frac{r^2 - \sigma^2}{r^2}\right) + \frac{\sigma^2}{2(r^2 - \sigma^2)} + \frac{\sigma^2}{2r^2} \right]$$

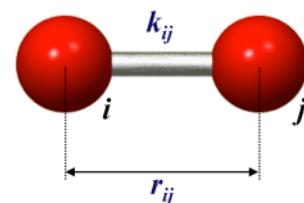
$$U_{LJ}^{repulsive}(r) = -\frac{A\sigma_{LJ}^6}{2520r} \left[\sigma^2 \left(\frac{1}{2(r-\sigma)^7} + \frac{1}{2(r+\sigma)^7} + \frac{1}{r^7} \right) - \frac{\sigma}{3} \left(\frac{1}{(r-\sigma)^6} + \frac{1}{(r+\sigma)^6} \right) - \frac{1}{15} \left(\frac{2}{r^5} - \frac{1}{(r-\sigma)^5} + \frac{1}{(r+\sigma)^5} \right) \right]$$

$$U(r) = U_{LJ}^{attractive}(r) + U_{LJ}^{repulsive}(r)$$

Agglomeration

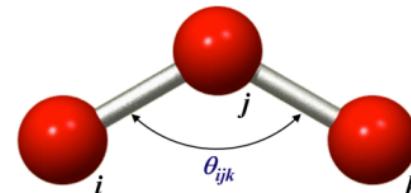
How to determine D_f ?

- connect colliding particles to each other with a single bond



$$U_{\text{harmonic-bond}} = \frac{1}{2} k_h (r_{ij} - r_0)^2; k_h = 2 E_{\text{adh}}^{JKR} / a^2; E_{\text{adh}}^{JKR} = \psi \pi a^2$$

- connection of 2 contacting particles with a single bond, 3rd particle with angle potential and 4th particle with dihedral potential

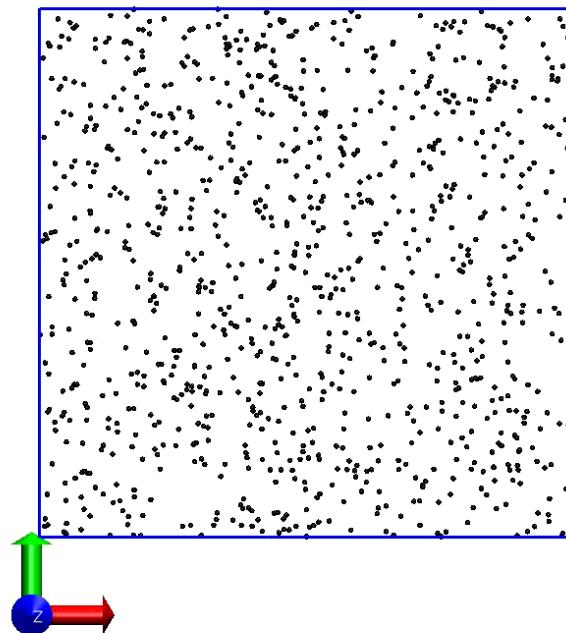


$$U_{\text{angular-bond}} = k_a (\theta - \theta_0)^2; k_a = \frac{k_0}{192}; k_0 = \frac{3\pi a^4 E_Y}{4(\sigma/2)^3}$$

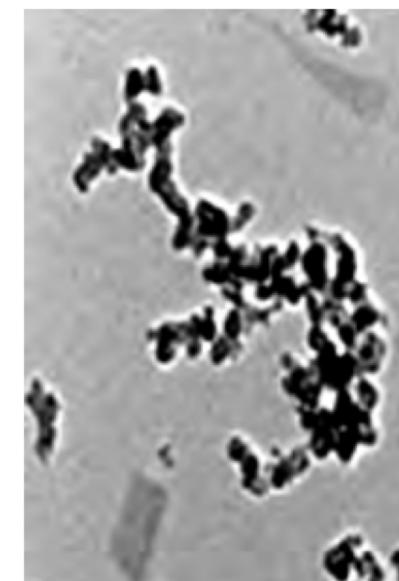
Agglomeration

Brownian Motion

LANGEVIN DYNAMICS



COMPARISON SIMULATION - EXP

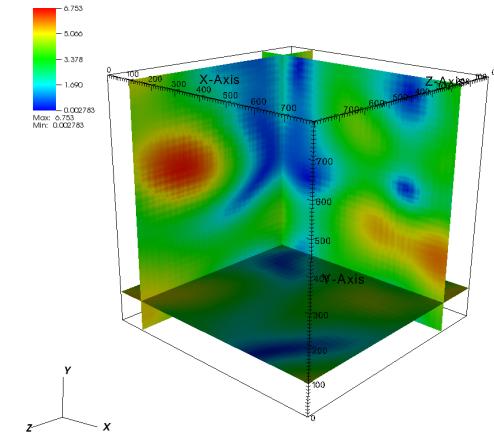


© Tumolva et al., 2010

Langevin Dynamics

Computations setup

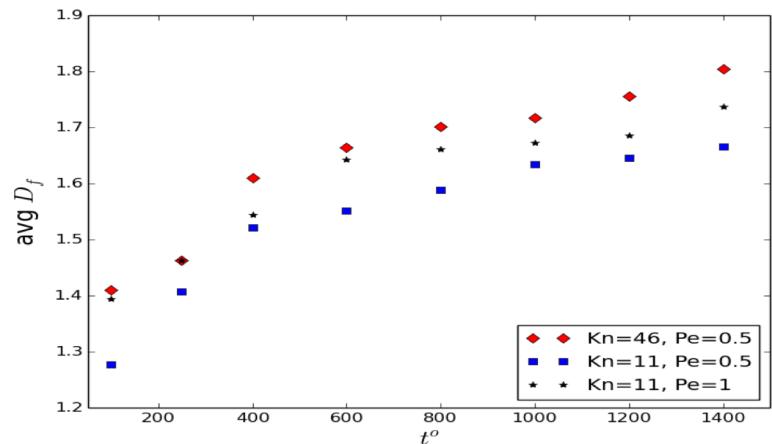
- Different primary particle sizes: $\sigma=5\text{nm}, 20\text{nm}, 100\text{nm}$
- Domain size: 800σ
- Number of particles: $N_p=3.2 \cdot 10^6$
- Volume fraction: $f_v=0.00625$
- Superposed flow field
- Number of simulations per case: $N_s=5$
- Run times: 20,000 – 43,000 CPUh per run to reach $t^0=1500$.



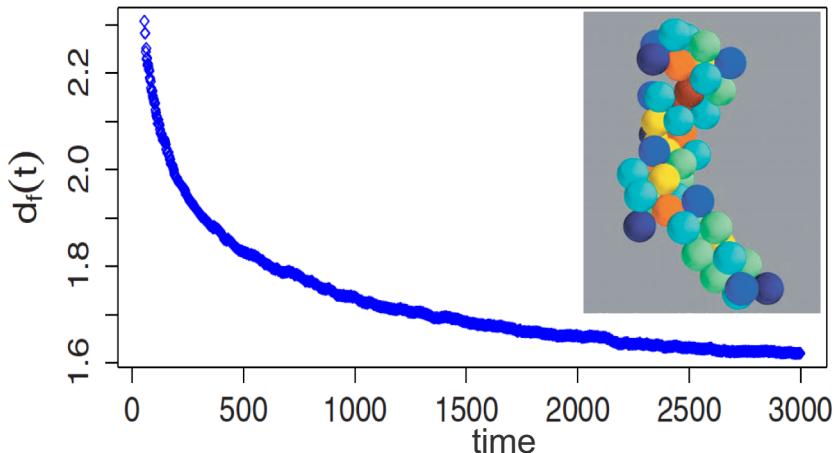
	C1	C2	C3	C4	C5	C6	C7	C8	C9
σ [nm]	5			20			100		
ϵ [m^2/s^3]	$4.5 * 10^9$	$1.1 * 10^{11}$	$4.5 * 10^{11}$	$1.1 * 10^8$	$2.7 * 10^9$	$1.1 * 10^{10}$	$6.9 * 10^3$	$1.7 * 10^5$	$6.9 * 10^5$
τ_{BM} [s]	$1.1 * 10^{-9}$	$1.1 * 10^{-9}$	$1.1 * 10^{-9}$	$6.8 * 10^{-8}$	$6.8 * 10^{-8}$	$6.8 * 10^{-8}$	$8.6 * 10^{-6}$	$8.6 * 10^{-6}$	$8.6 * 10^{-6}$
τ_{kol} [s]	$1.1 * 10^{-7}$	$2.1 * 10^{-8}$	$1.1 * 10^{-8}$	$6.8 * 10^{-7}$	$1.4 * 10^{-7}$	$6.8 * 10^{-8}$	$8.6 * 10^{-5}$	$1.7 * 10^{-5}$	$8.6 * 10^{-6}$
Kn [-]	46	46	46	11	11	11	2	2	2
Pe [-]	0.1	0.5	1	0.1	0.5	1	0.1	0.5	1

Results: Langevin Dynamics

Temporal evolution of average D_f

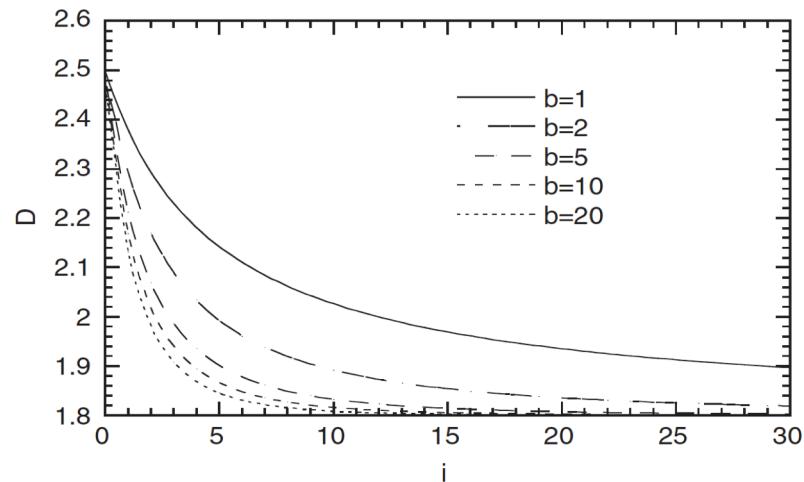


OUR WORK

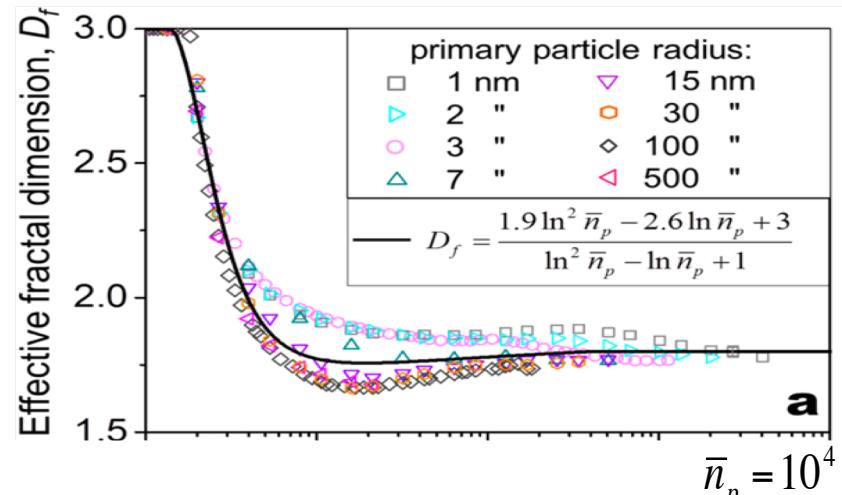


ISELLA & DROSSINOS (PRE, 2010)

University of Stuttgart



KOSTOGLOU ET AL. (AS, 2006)

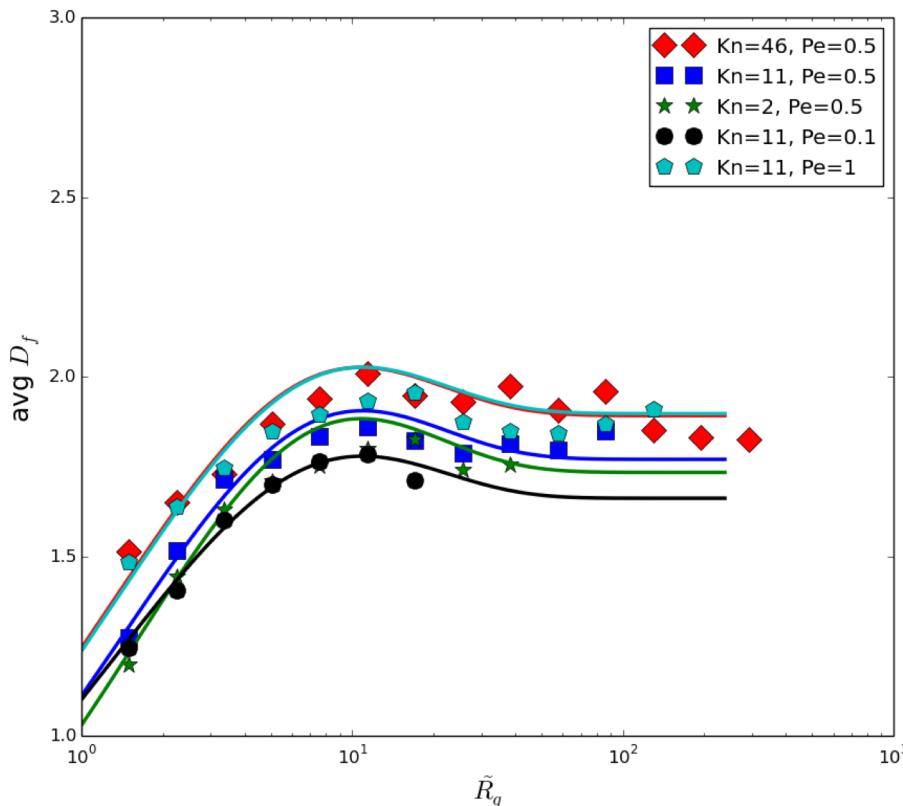


GOUDELI ET AL. (LANGMUIR, 2015)

Results: Langevin Dynamics

Attempt modelling

DEPENDENCE OF $D_f = D_f(R_g)$ (NO REAL TIME DEPENDENCE)



MODELLING

- Functional dependence

$$D_f(\tilde{R}_g) = f_1 + f_2 = c_1(1 - e^{-c_2 \tilde{R}_g^{c_3}}) - c_4(1 - e^{-0.08 \tilde{R}_g}).$$

- Modelling constants

constant	modelling assumption	value of coefficients
two-function model		
c_1	DLA limit (cluster - particle)	2.5
c_2	$f_1 + f_2 = D_f(1)$	-
c_3	$\frac{\partial D_f}{\partial \tilde{R}_g} _{\tilde{R}_g=11} = 0$	-
c_4	DLA limit (cluster-cluster)	0.62
$D_f(1)$	$a - \frac{b}{1+(cPe)^d + (eKn)^f}$	a=1.25, b=0.25, c=1.5, d=7, e=0.08, f=3

- Does not yet help us with assessment of β

Langevin Dynamics

Issues

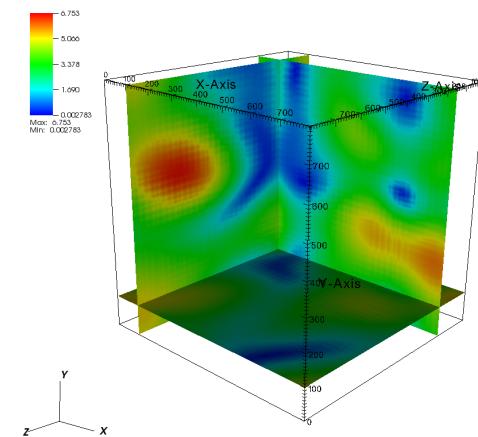
- Moderately expensive
 - Scale separation – we cannot fully bridge the gap between turbulence scales and particle size
 - Statistics poor, especially for large clusters
 - Very limited info on collision frequencies
- Need scale preservation and need to get “bigger”
- 1) use brute force or
2) use coarse graining approach

Langevin Dynamics

Scale Preserving Simulations

- What do I mean with scale preserving?
 - Typical particle size: $\sigma = 20 \text{ nm}$
 - Typical Kolmogorov size: $\eta_{\text{Kol}} = 2 \mu\text{m}$
 - Turbulent length scale: $l_t > 20 \mu\text{m}$
 - Domain size: $L > 40 \mu\text{m}$
- Solution above (as $L/\sigma=800 < 2000$):
 - rescale DNS turbulence field
 - Cannot keep ratio of η_{Kol}/σ
 - Scaling of gradients (preserve small scale shear)
 - Preserve dissipation

(and this is small, C6)



$$\frac{l_0}{t_0} = \text{const}$$

$$\varepsilon = \hat{\varepsilon} \frac{l_0^2}{t_0^3} = \hat{\varepsilon} \frac{u_0^3}{l_0}$$

Langevin Dynamics

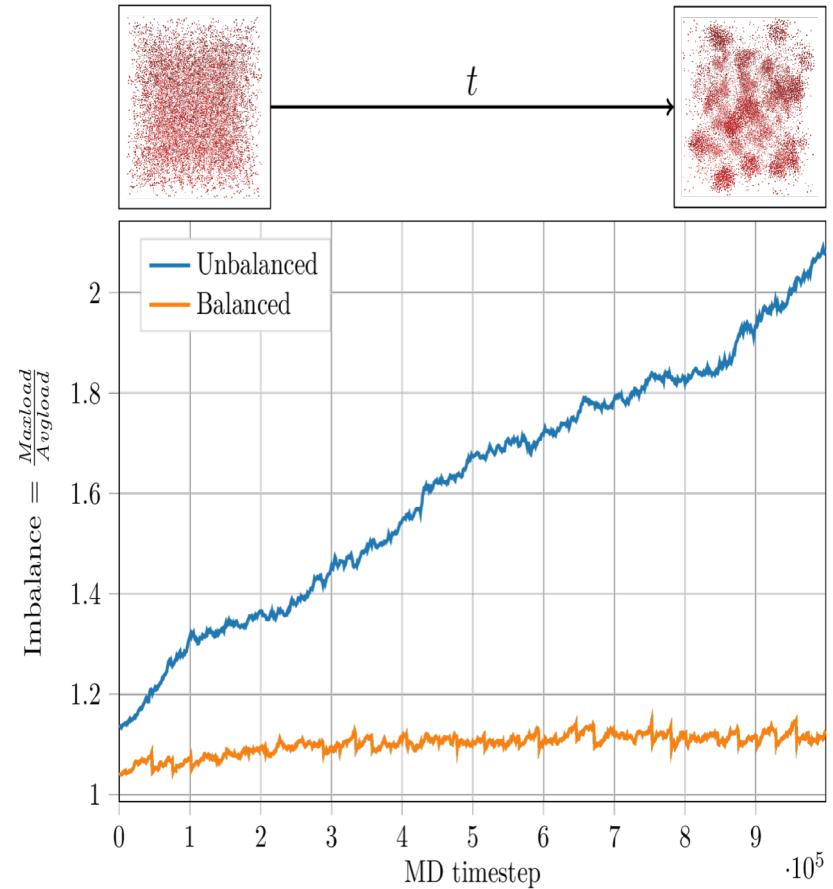
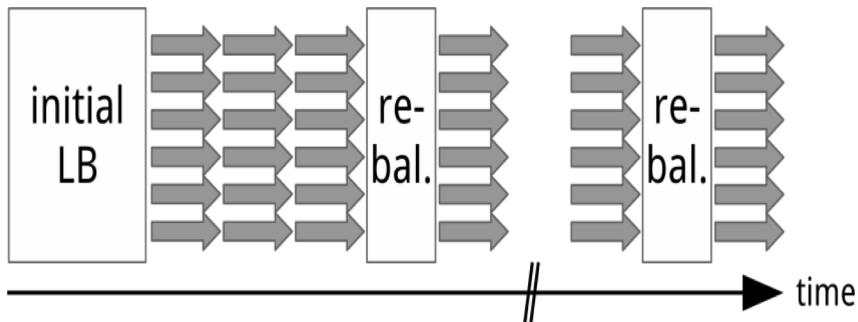
Large Scale Computations

- 1st strategy – make the computations bigger
 - What is doable?
 - $L = 2600 \sigma$
 - $N_p = 110 \cdot 10^6$
 - $t_{\text{end}} = 1200 t_{\text{LD}}^0$
 - Computational time ~ 2 million core hours – if computations scale
 - But: computational efficiency is the issue

Large Scale Computations

Load Balancing

- MD simulations on multiple processes:
 - Slowest process determines overall runtime
 - Degrading parallel performance for inhomogeneous particle distributions
 - Indicator: imbalance amongst processes
- Remedy:
 - Change subdomains to balance load



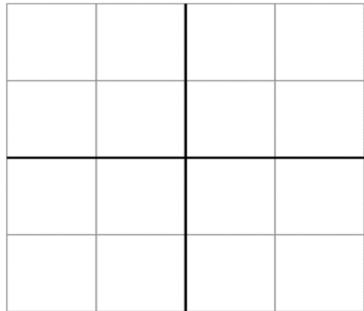
10,000 initially homogeneously distributed Lennard-Jones particles on 8 processors.
Graph shows imbalance amongst subdomains.

Large Scale Computations

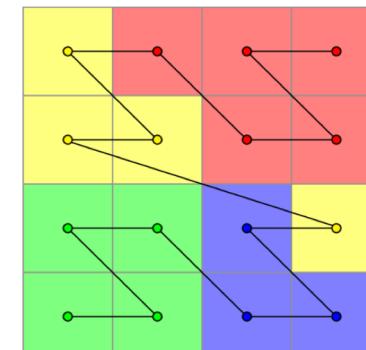
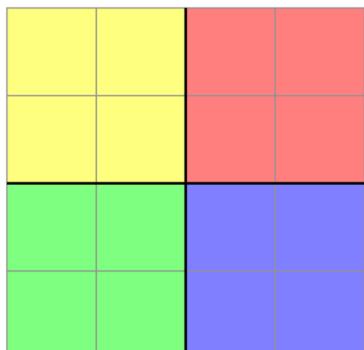
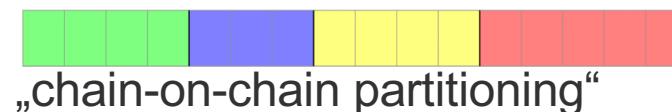
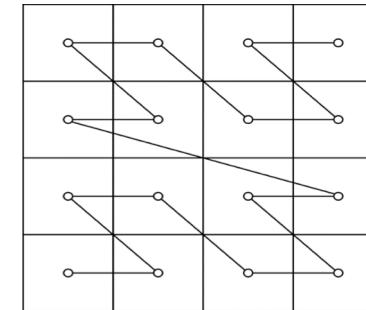
Load Balancing

- Methodology of partitioning

Default: equally sized boxes on grid



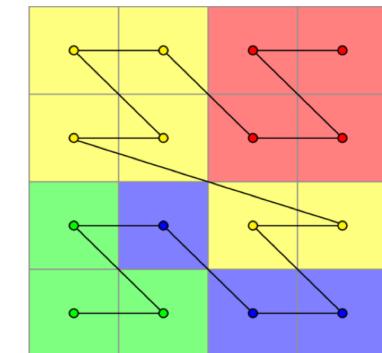
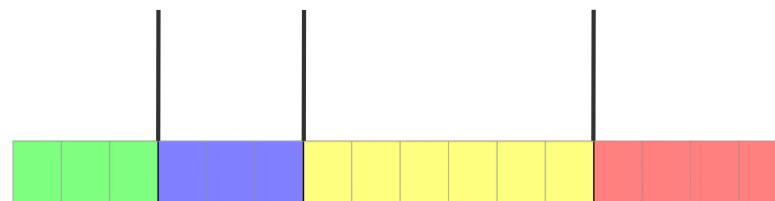
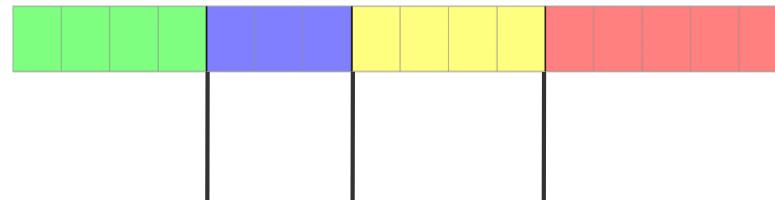
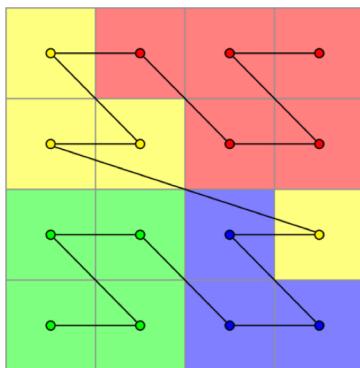
SFC-based partitioning: subdomains defined via linearization of the domain



Large Scale Computations

Load Balancing

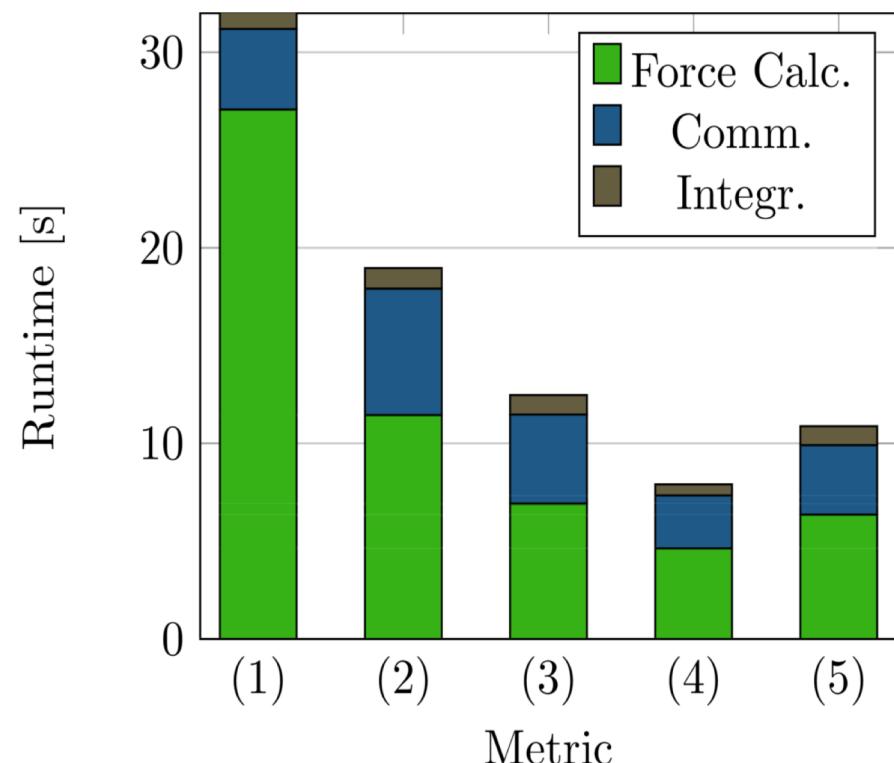
- Repartitioning:
 - Associate a weight w_i with each cell
 - Determine new partition boundaries in 1d -> load of each process is approximate average process load $1/P \sum_i w_i$ for P processes



Large Scale Computations

Load Balancing

- Results
 - Evaluation of end state of particle agglomeration with 3.2 million particles
 - Runtime of 1,000 MD time steps on 2,400 cores on HazelHen



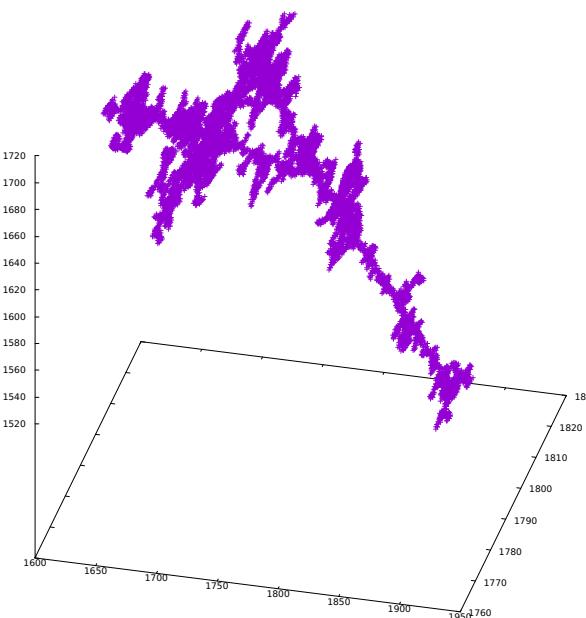
Weights from left to right:

- (1) Without repartitioning,
- (2) # LJ distance calculations,
- (3) # LJ force pairs
- (4) # particles,
- (5) # bonded interactions.

Large Scale Computations

Issues

- Works on ~ 10,000 cores pretty well
- $L=2600\sigma$ and 110M particles → larger scales give larger velocities/forces

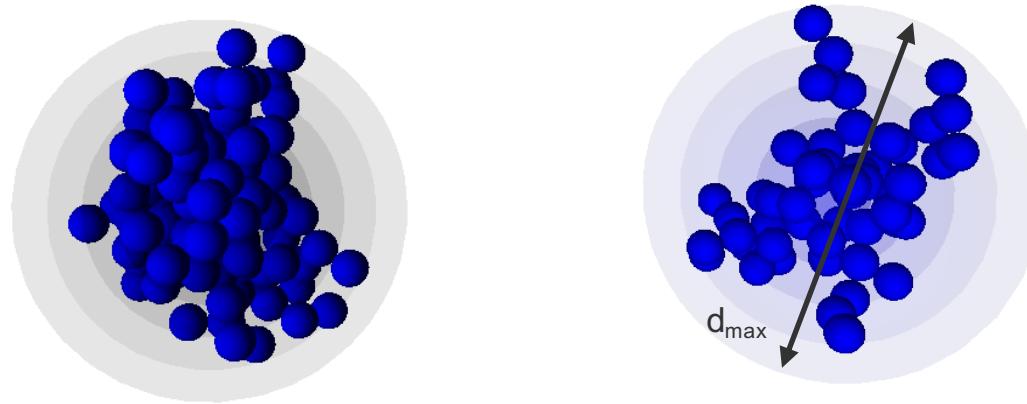


→ need to introduce breakage
hope to show results on next conference

Coarse-Graining (CG)

Benefits/Drawbacks

- **2nd strategy** – coarse graining: Replace agglomerate by single coarse-grained particle



- Benefits
 - Increase number of particles, increase size of aggregates, increase domain size, increase width of turbulence spectrum
- Drawbacks
 - loss of detail, introduce additional characteristics for CG particle, quantification of characteristics requires large number of simulation

Coarse-Graining

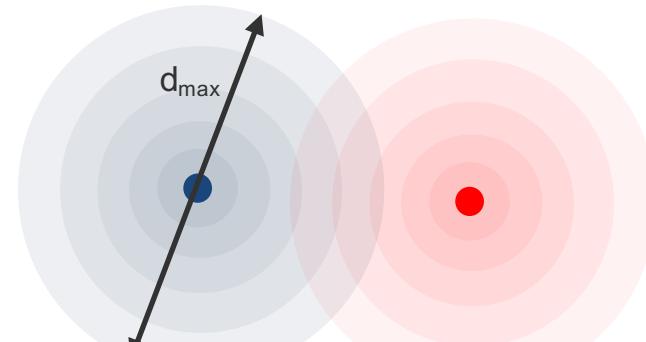
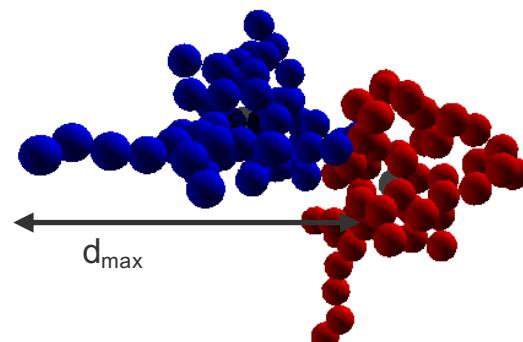
Collision probability

- Characteristics of CG particle

- Mass
- Drag coefficient
- Representative size
- Morphology
- Collision frequency

$$\rightarrow \begin{aligned} m_{CG} &= i \cdot m_p \\ \gamma_{CG} &= 3\pi\mu_f i\sigma_p \\ \sigma_{CG} &= d_{max} \\ D_f &= \text{const} \\ P_{coll} &\text{ is modelled} \end{aligned}$$

- CG particle with d_{max} - not every overlap leads to a collision

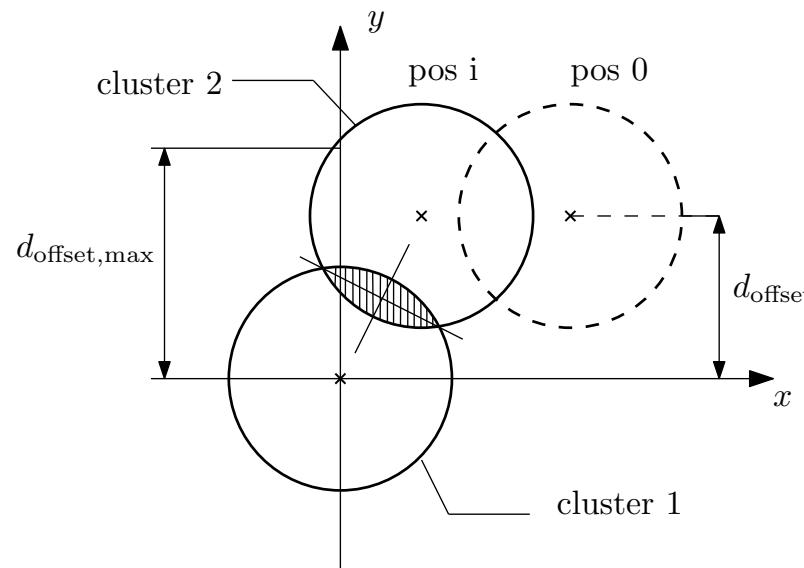


- Introduce collision probability as function of passing distance

Coarse-Graining

Collision probability

- Collision probability as function of passing distance
 - place 1st agglomerate at (0,0) and rotate randomly
 - place 2nd agglomerate at (d_{\max} , d_{offset}) and rotate randomly
 - move 2nd cluster parallel to x-axis
 - record probability of collision

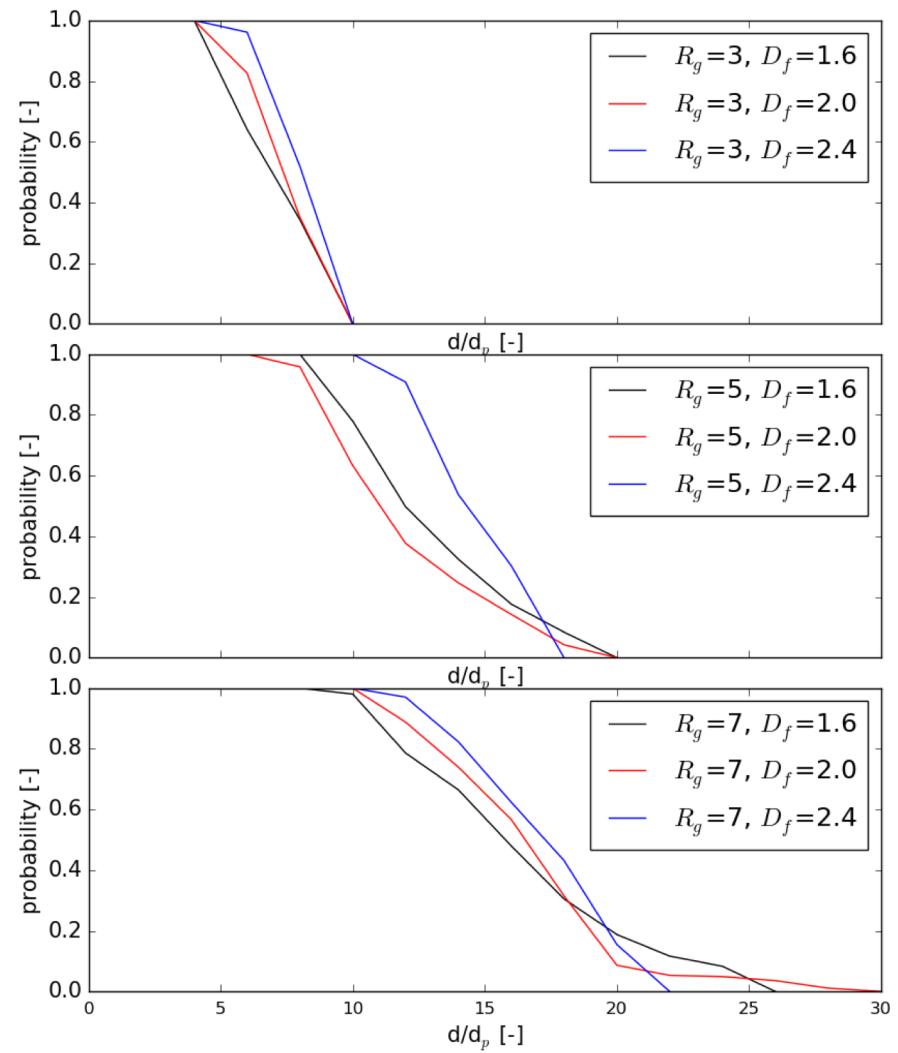


Coarse-Graining

Collision probability

- 9 cases

Represent. agglomerate	N	R_g	D_f
	39	~3	~1.6
	55	~3	~2.0
	100	~3	~2.4
	106	~5	~1.6
	128	~5	~2.0
	205	~5	~2.4
	145	~7	~1.6
	207	~7	~2.0
	309	~7	~2.4



Coarse-Graining

Modelling

- Represent agglomerate by radial density function $\rho(r)$

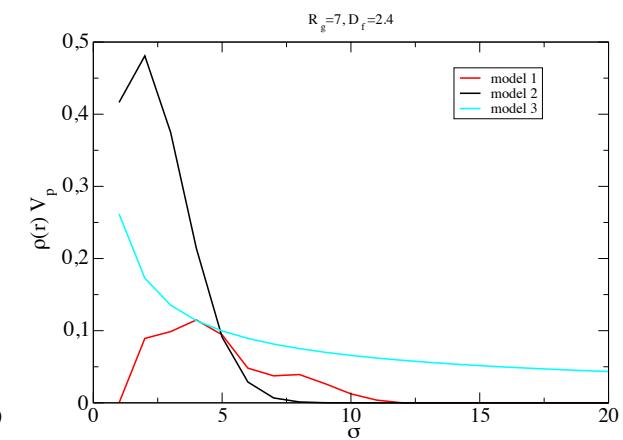
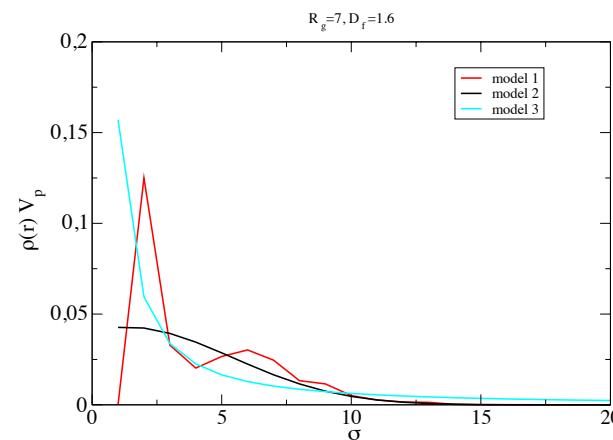
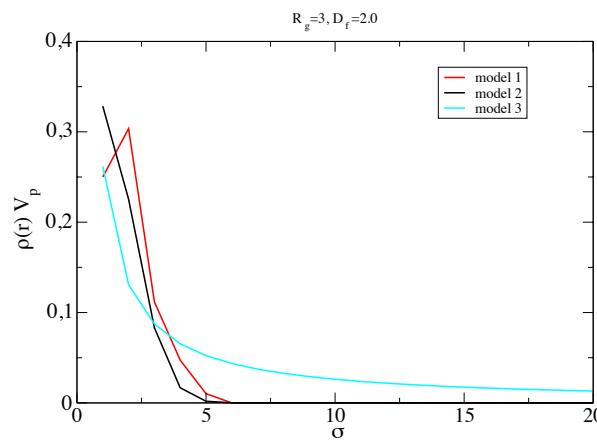
- Model 1 – real radial density function

- Model 2 – Lattuada et al. (2004)

$$\rho(r) = Ar^\beta \exp\left[-\left(\frac{r}{R_c}\right)^z\right] \text{ with } R_c = pR_p i^{1/D_f}$$

- Model 3 – Rogak & Flagan (1990)

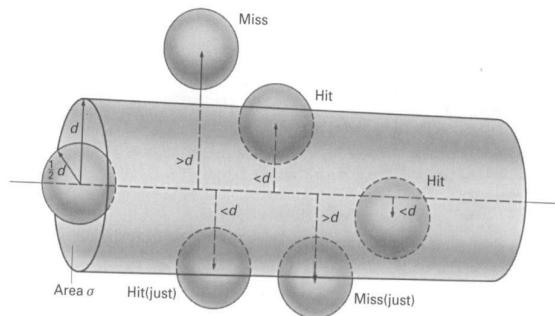
$$\rho(r) = Cr^{D_f - 3}$$



Coarse-Graining

Modelling

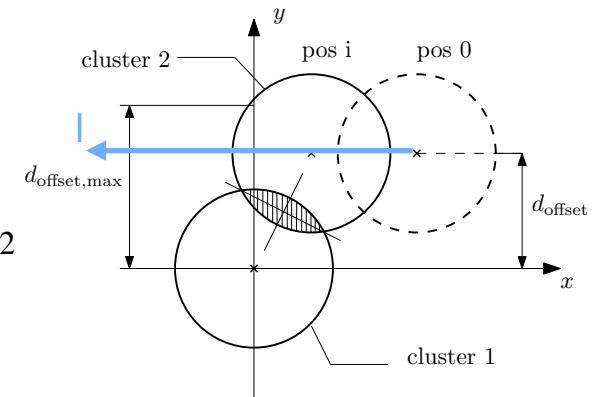
- Use ideas of kinetic gas theory to compute number of collisions



- Solve

$$P_{coll} = \int_{-\infty}^{\infty} \iiint_V \rho_1(r_1) \rho_2(r_2) \pi \sigma_p^2 dx dy dz dl$$

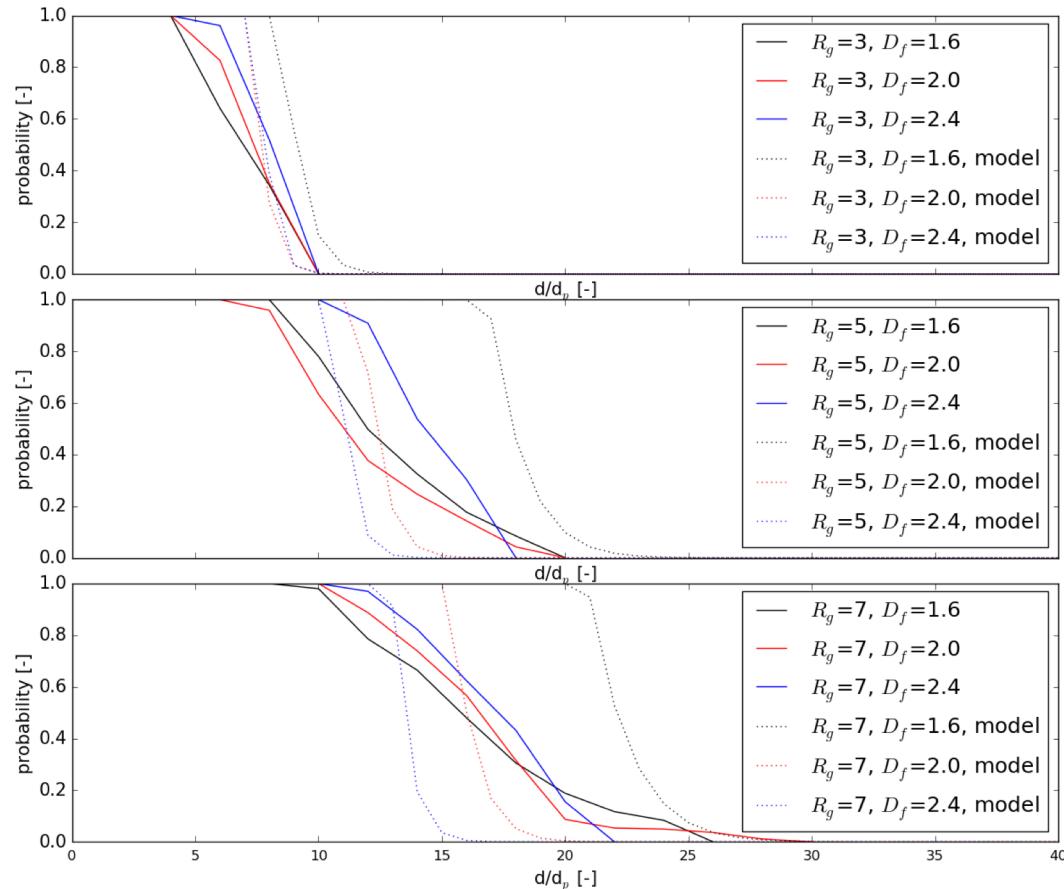
$$\text{with } r_1^2 = x^2 + y^2 + z^2 \text{ and } r_2^2 = (x - l)^2 + (y - d_{offset})^2 + z^2$$



Coarse-Graining

Collision Probabilities

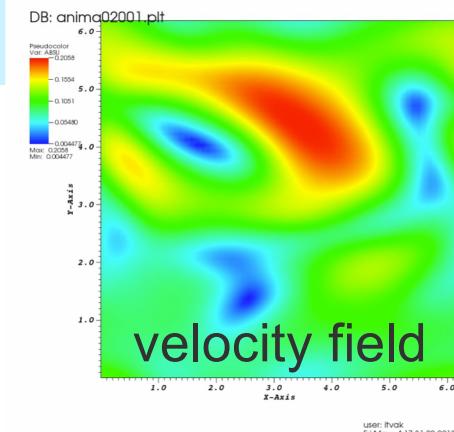
- Direct simulations vs. model 2



Coarse-Graining

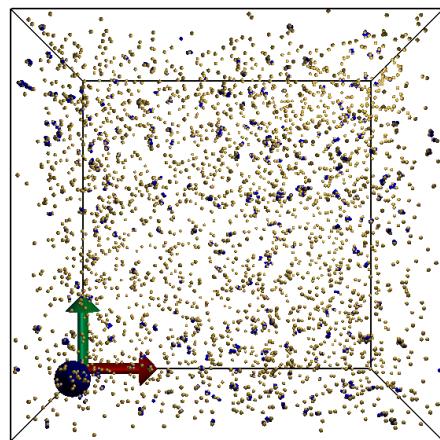
The setups

- Simulations for $R_g=3$, $D_f=1.6$, case C8 ($\sigma=100\text{nm}$)

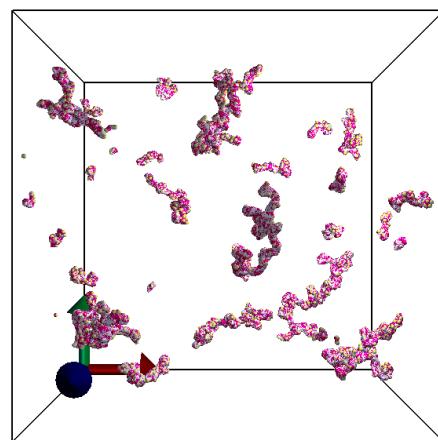


Detailed LD

early time

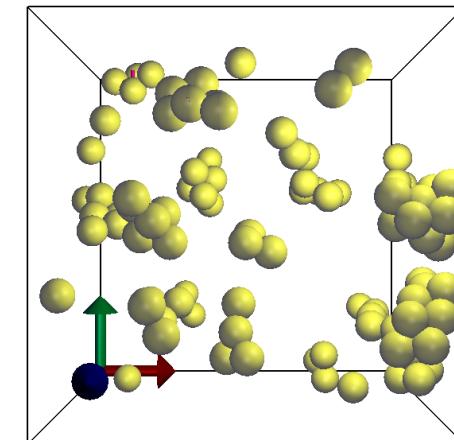


late time



coarse grained

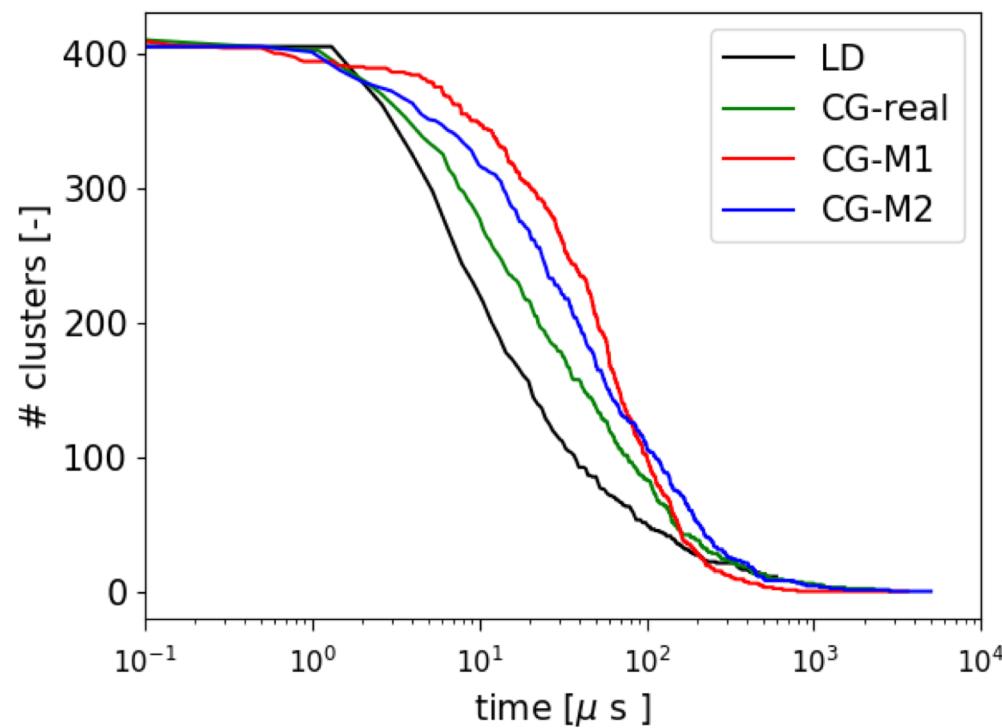
late time



Coarse-Graining

Results

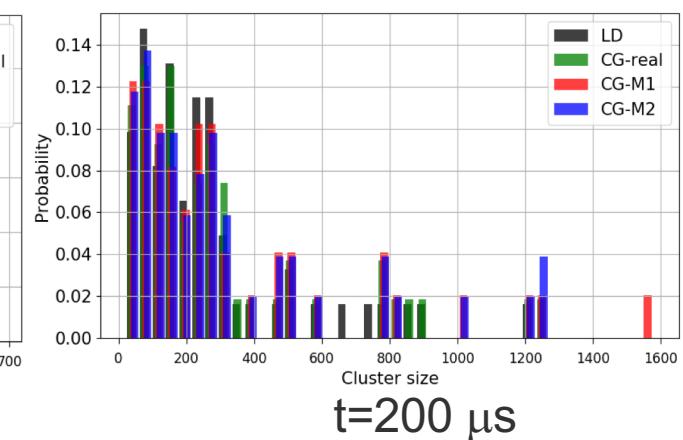
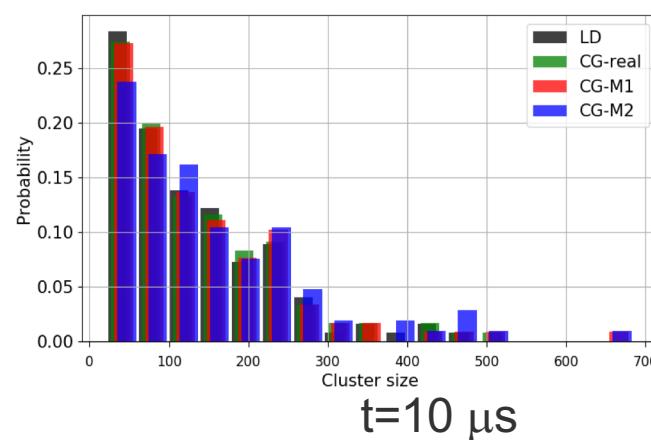
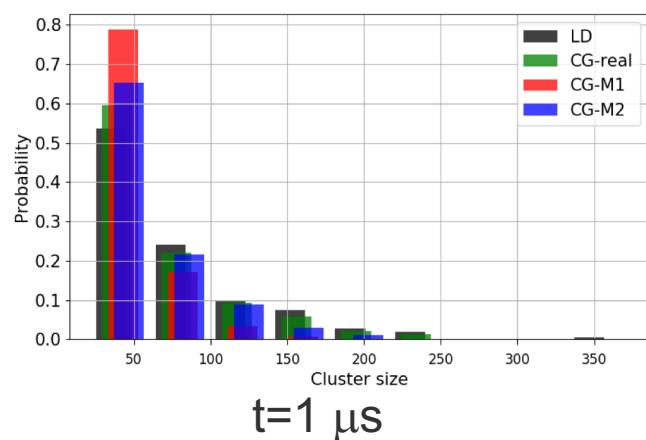
- Number of clusters for $R_g=3$, $D_f=1.6$



Coarse-Graining

Results

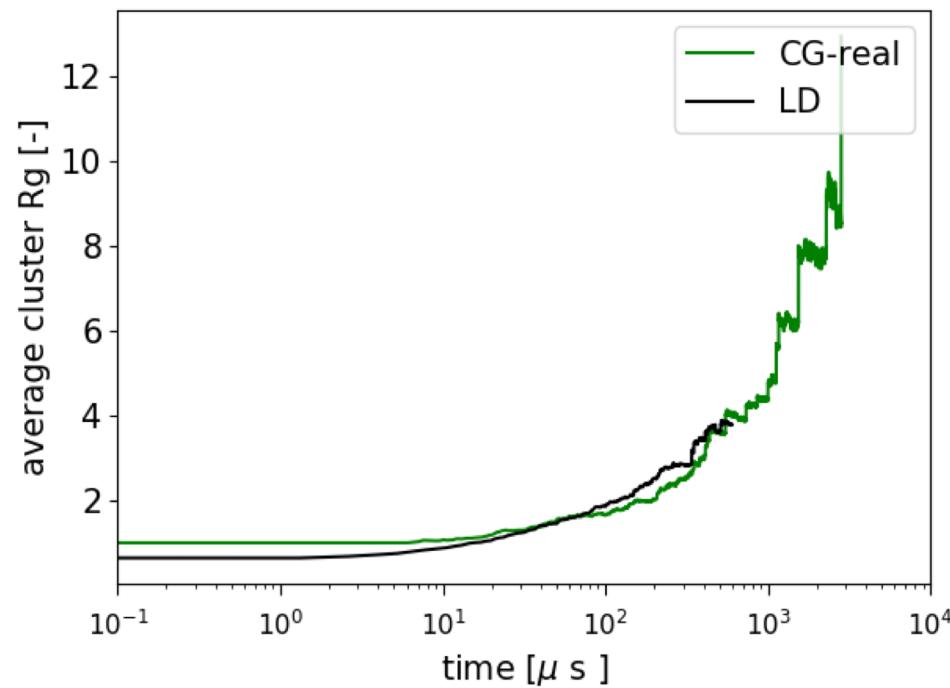
- PSD at different times ($R_g=3$, $D_f=1.6$)



Coarse-Graining

Results

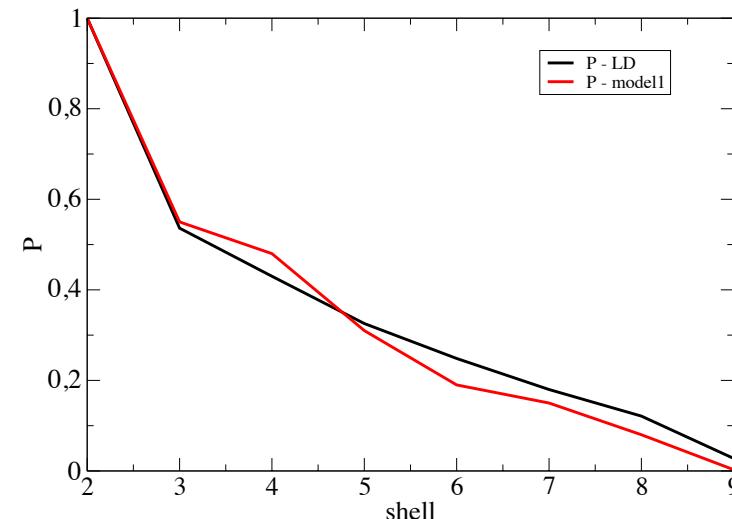
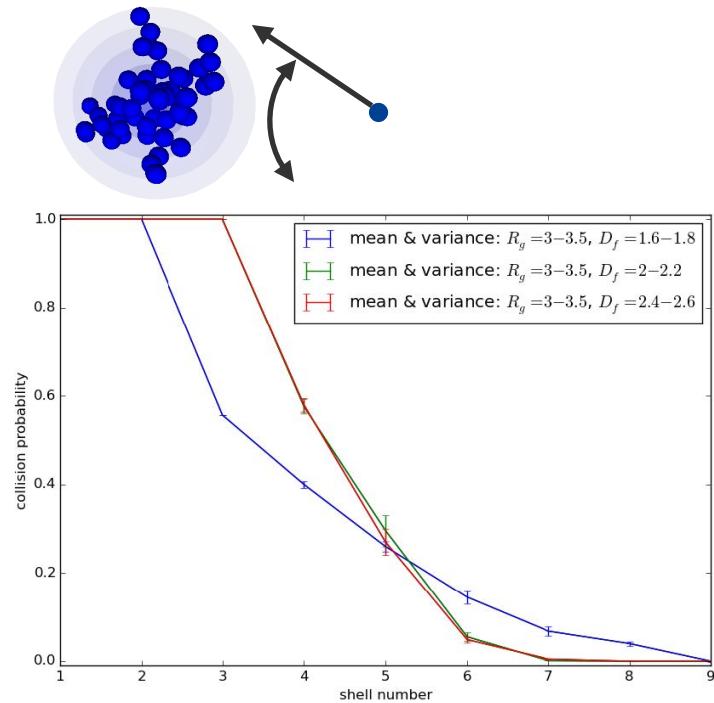
- Average cluster size ($R_g=3$, $D_f=1.6$)



Coarse-Graining

Further steps

- Results semi-successful for modelled radial densities – why?
- Results **good** if correct collision probability used, but what about ...
 - Large uncertainty when basing the analysis on individual clusters
 - Find appropriate characteristics for an average agglomerate of R_g and D_f
 - For collision statistics between single particle and cluster:



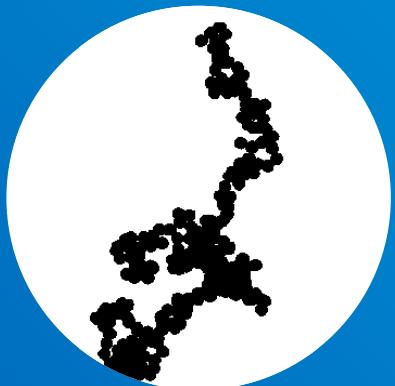
Summary

... and future work

- Achievements
 - Modified MD code to account for particle agglomeration
 - Parameterization of D_f as function of R_g (and turbulent advective field)
 - Lack of sufficient statistics leads to coarse-graining
 - Major issue: collision probability for CG particle
 - Functional dependency computed
 - Functional dependency modelled
 - Large scale computations set up and appropriate CG model proposed
- Issues to be solved in future work
 - Large scale computations for CG validation
 - Varying CG particles
 - Non-sphericity of CG particle
 - Compare new expression with standard expressions for collision kernels



Thank you!



Literature

G. Inci, A. Arnold, A. Kronenburg, and R. Weeber, "Modelling nano-particle agglomeration using local interactions". *Aerosol Sci. Technol.*, 48:8, 842-852 (2014), DOI: [10.1080/02786826.2014.932942](https://doi.org/10.1080/02786826.2014.932942).

G. Inci, A. Kronenburg, R. Weeber and D. Pflueger, "Langevin Dynamics simulation of transport and aggregation of soot nano-particles in turbulent flows", *Flow Turbul. Combust.* (2017). DOI: [10.1007/s10494-016-9797-3](https://doi.org/10.1007/s10494-016-9797-3)

Acknowledgements:

G. Inci, R. Weeber, A. Arnold, C. Holm
Funded by DFG under grant number SFB-716/A8