

# Flowfield and Flame Structure during Thermoacoustic Intermittency

Experimental and Computational Study in a Turbulent Swirl Stabilized  
Combustor

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## Focal points

- Intermittency: precedes triggering of thermoacoustic oscillations (limit cycle).
- Intermittent bursts arise stochastically, hence it is difficult to predict their occurrence.
- It is important to gain knowledge of the flow/combustion phenomena causing the intermittent bursts.

### Focal points:

- The flame precesses under the influence of the PVC before intermittent thermoacoustic bursts.
- The flame front becomes increasingly more wrinkled during transition into intermittency.

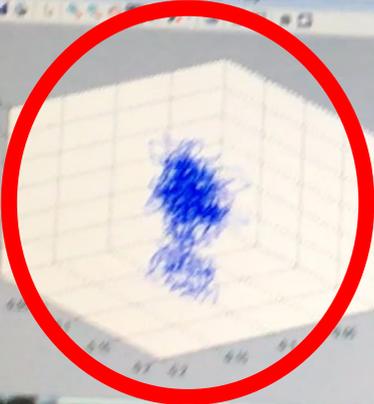
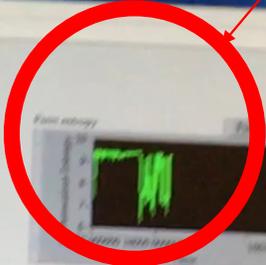
## Structure

- **Model** gas turbine **configuration** and experimental instrumentation.
- **Isothermal** flow structure and quiescent flow and flame structure
- Flame and **flowfield structure** during **intermittent** transitions into thermoacoustic instabilities
- (Link between thermoacoustic dynamics and flame front curvature).
- **Calculation** of this flow



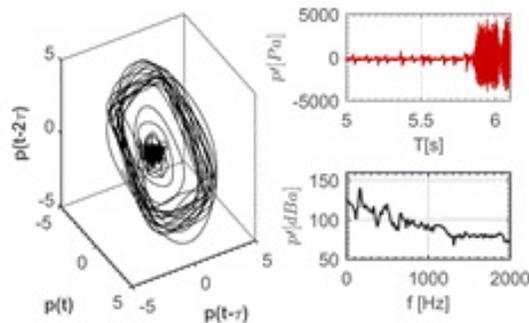
Unstable Premixed Flame

Forewarning  
Signal

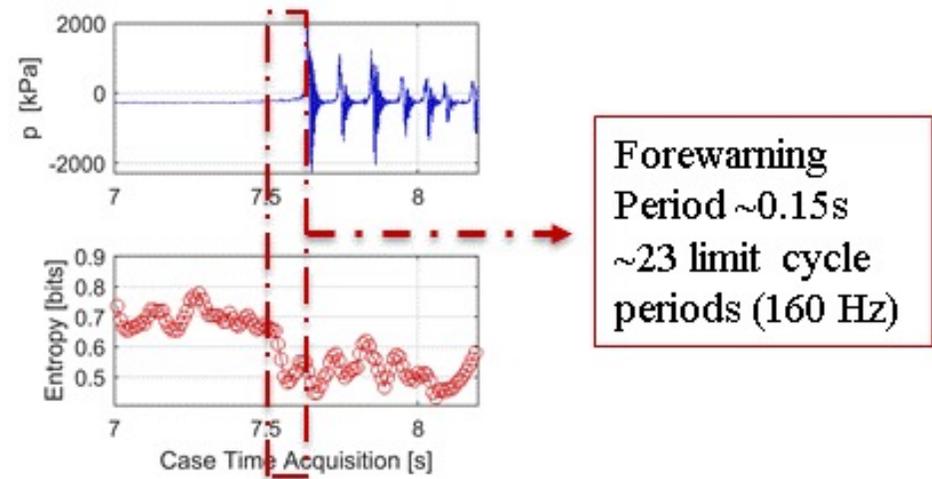


Topology of attraction of dynamic pressure signal in phase space  
Axis auto adjusted scaling

Intermittency



Permutation Entropy (forewarning method)



- Short term prediction techniques such as the permutation entropy are employed to detect the triggering of a thermoacoustic instability.

## Description of dynamic states: Focus on the intermittent regimes

### Global operational quantities:

Bulk Reynolds number  $Re = 19000$   
Equivalence ratio  $\phi = 0.55$

On increasing extinction strain rate, the dynamics are driven from quiescent through intermittency into a limit cycle.

Karlis, E., Liu, Y. Hardalupas, Y., & Taylor, A. M. (2019d)

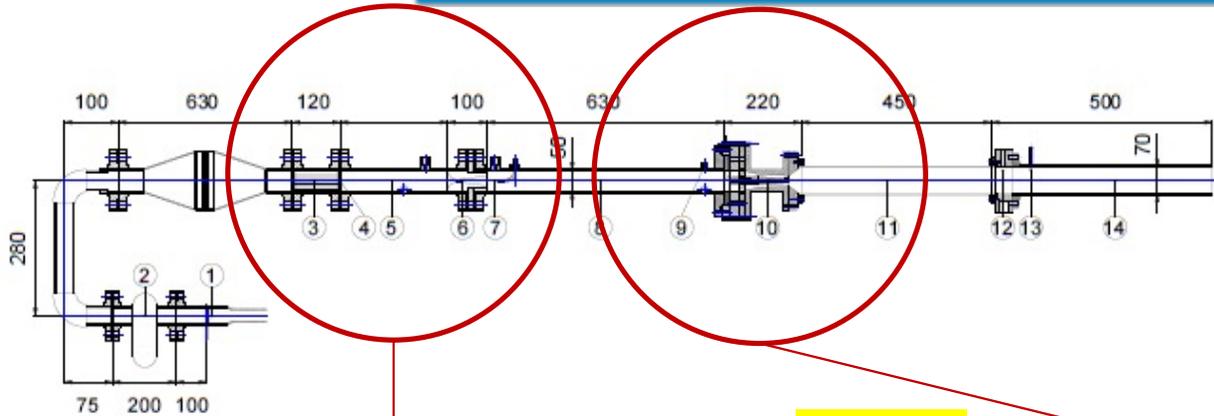
$H_2$  enrichment of  $CH_4$  blends in lean premixed gas turbine combustion. Fuel, 254, 115524

Mixture ID	Methane molar percentage $\chi:CH_4$	Hydrogen molar percentage $\chi:H_2$	Extinction Strain Rate [1/s]	Dynamic State
Case A	1.000	0.000	273	Susceptible to blow off
Case B	0.900	0.100	652	Quiescent, lifted
Case C	0.800	0.200	759	Quiescent, lifted
Case D	0.700	0.300	1127	Intermittent
Case E	0.650	0.350	1250	Intermittent
Case F	0.625	0.375	1350	Intermittent
Case G	0.600	0.400	1540	Limit Cycle

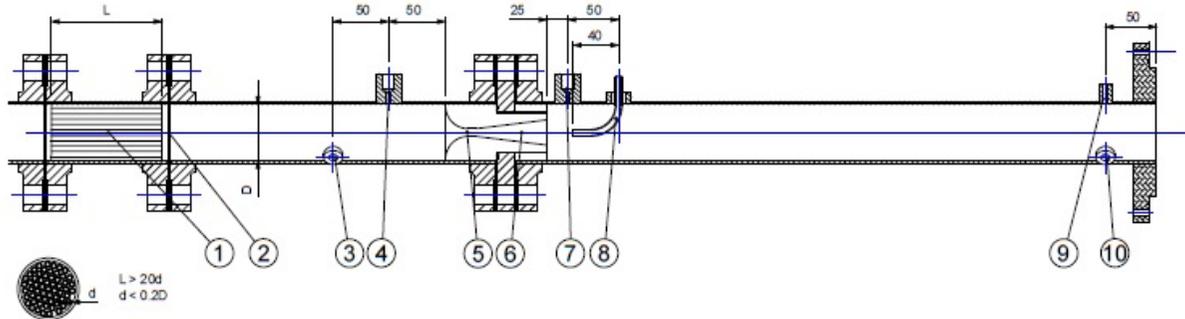
## Experimental configuration-Instrumentation

# Experimental Configuration

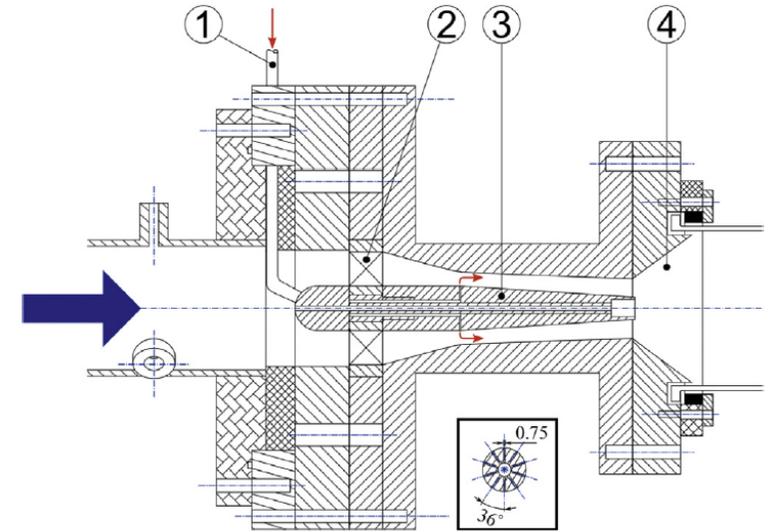
## Boundary Conditions



Venturi Nozzle: Choked  
Air Flow

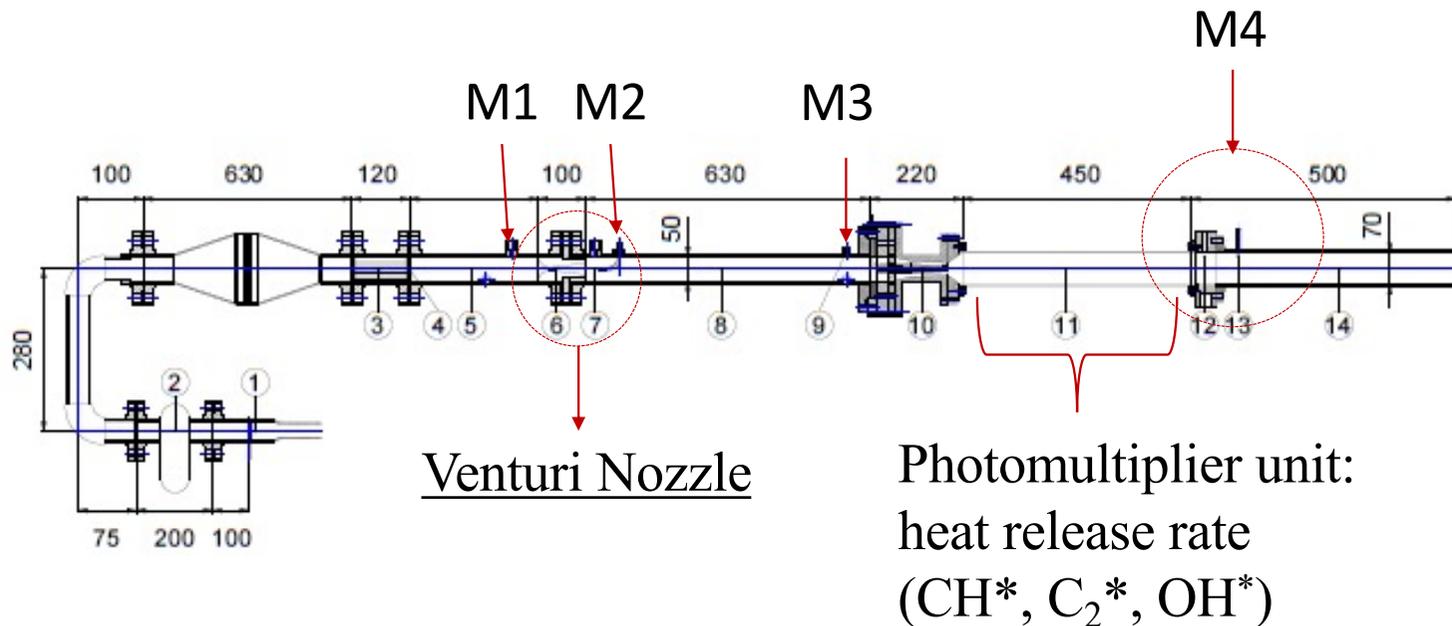


Burner: Choked Fuel  
Injection



## Experimental Configuration

Measurement of fundamental quantities



M1, M2: Monitor pressure drop across Venturi nozzle.

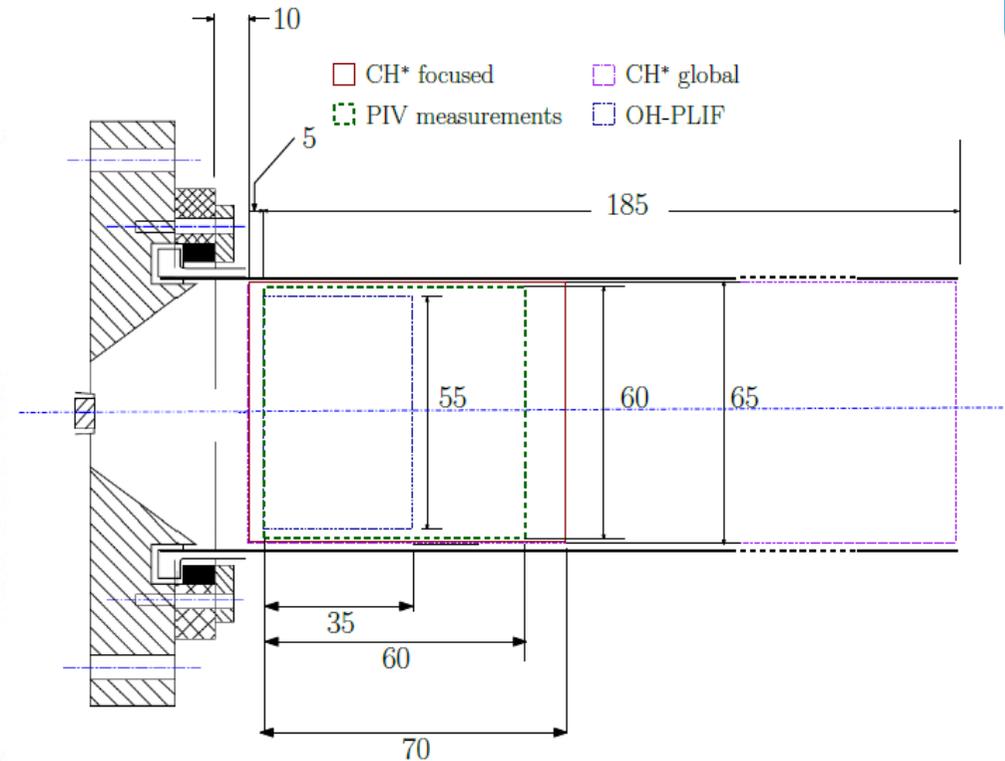
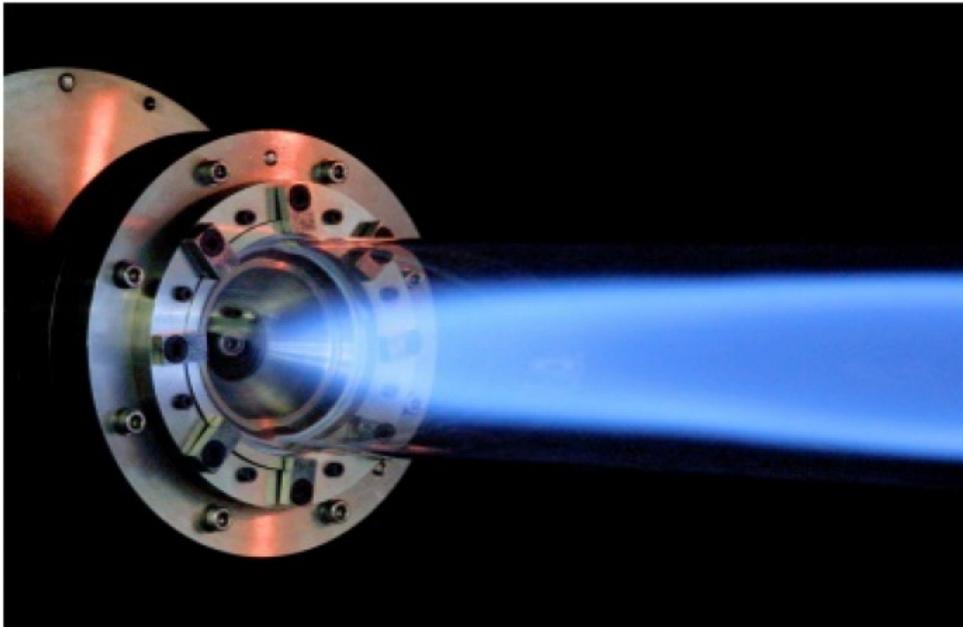
M2, M3: Acoustic wave amplitude inside duct (2-mic method)

M4: Standing wave along combustor

M5 (not shown): Pressure in fuel supply line

# Experimental Configuration

## Swirler and Optically Accessible Combustion Window

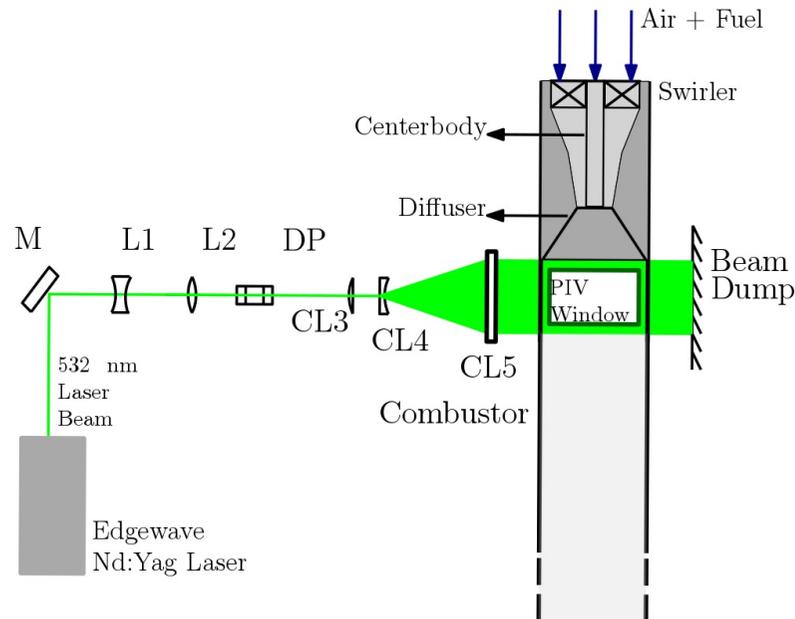


Measurement techniques: High speed CH\* imaging (3000 Hz), High speed PIV (3000 Hz), OH-LIF (phase conditioned with acoustics)

# Experimental Configuration

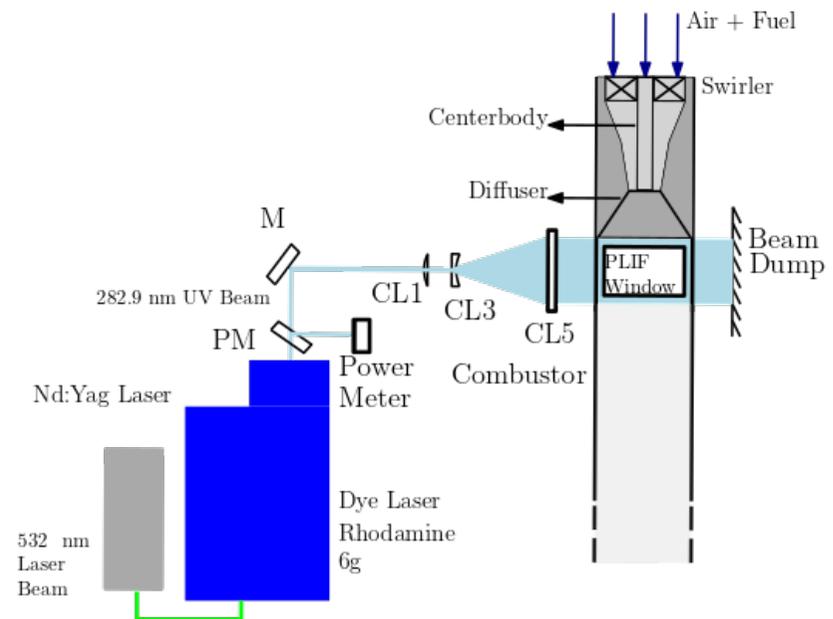
## Swirler and Optically Accessible Combustion Window

### PIV Optical Configuration



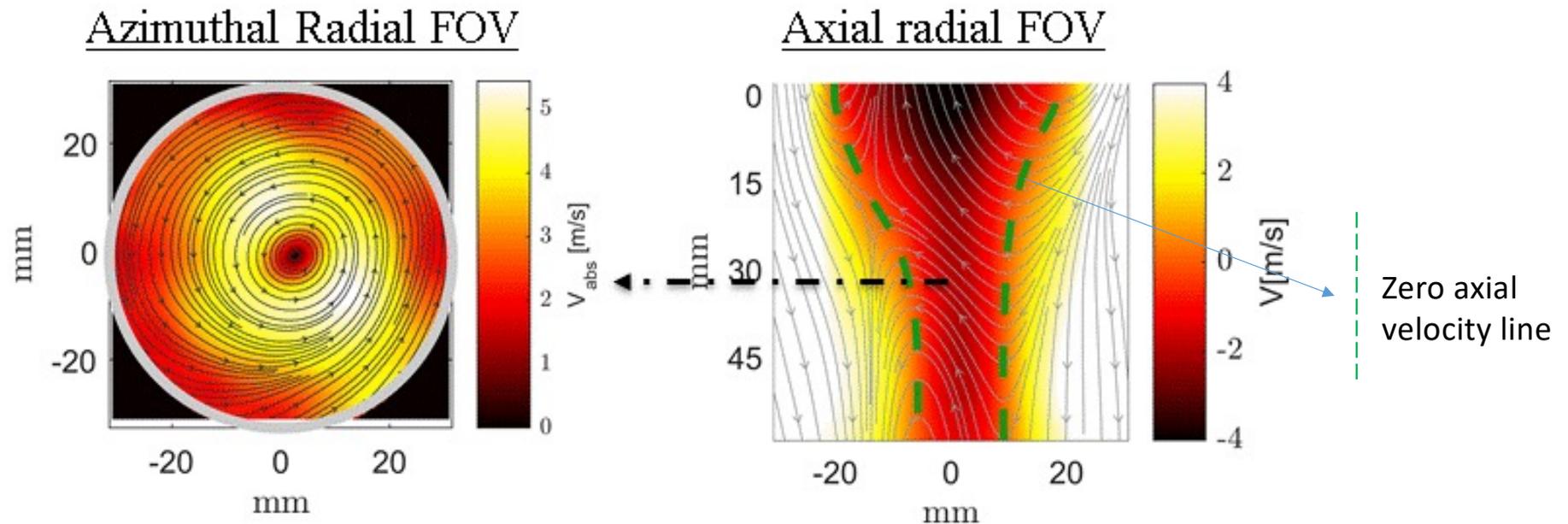
$dt=4\mu\text{s}$ , 3000 Hz, FOV: 60 mm x 60 mm, Interrogation windows 16 x 16 pixels, 75% overlap, Resolution: 0.23 mm, Nominal uncertainty: 0.06 m/s. Cut-off Lengthscale in the flow=0.20mm (Poinsot 1991).

### PLIF Optical Configuration



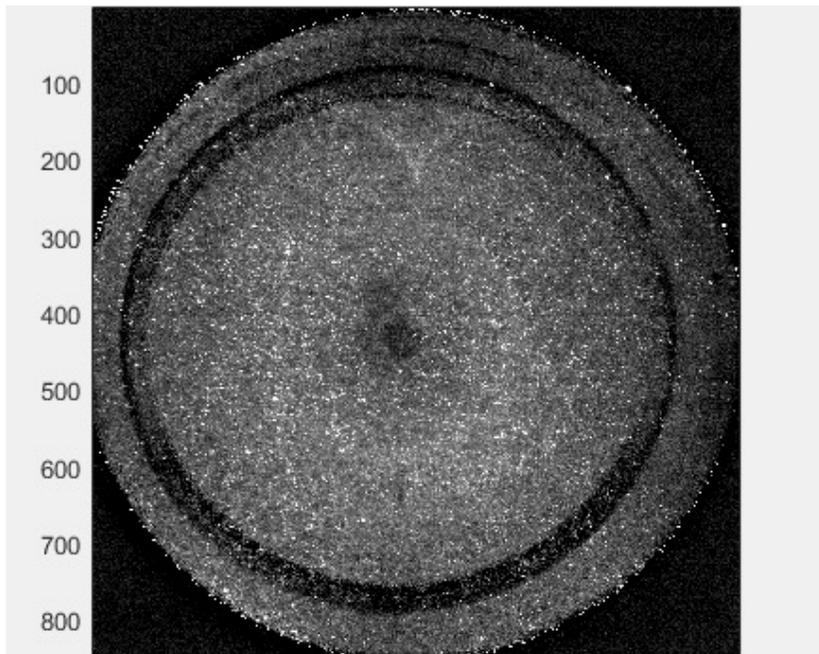
10 Hz, excitation  $Q_1(6)$  transition line:  $A^2\Sigma-X^2\Pi$  at 282.9 nm, light collected at 308 nm and 314 nm, dye laser output: 18mJ per pulse, field of view 35 mm x 35 mm, resolution of 5 line pairs / mm (curvature resolution)

Isothermal flowfield and quiescent flame structure



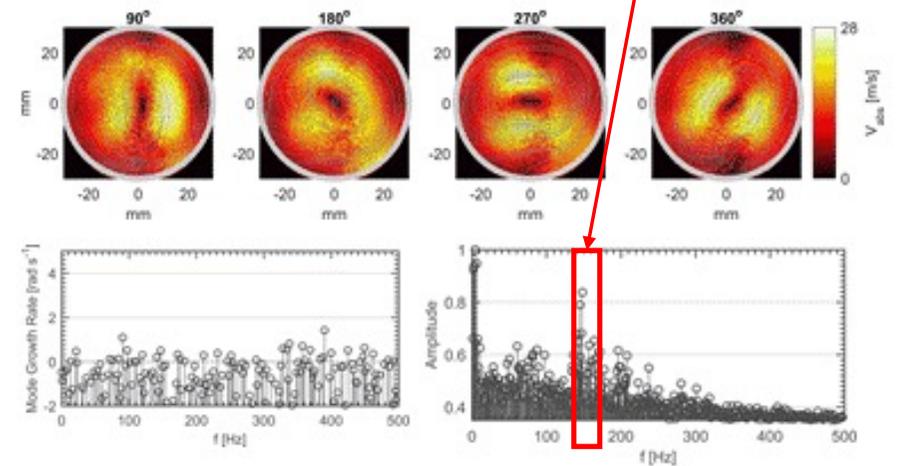
Axial-radial plane: isothermal flow features a recirculation zone with no downstream stagnation point, extending through all section of the PIV FOV

Mie Signal



DMD  
analysis

DMD Filtering at 140 Hz



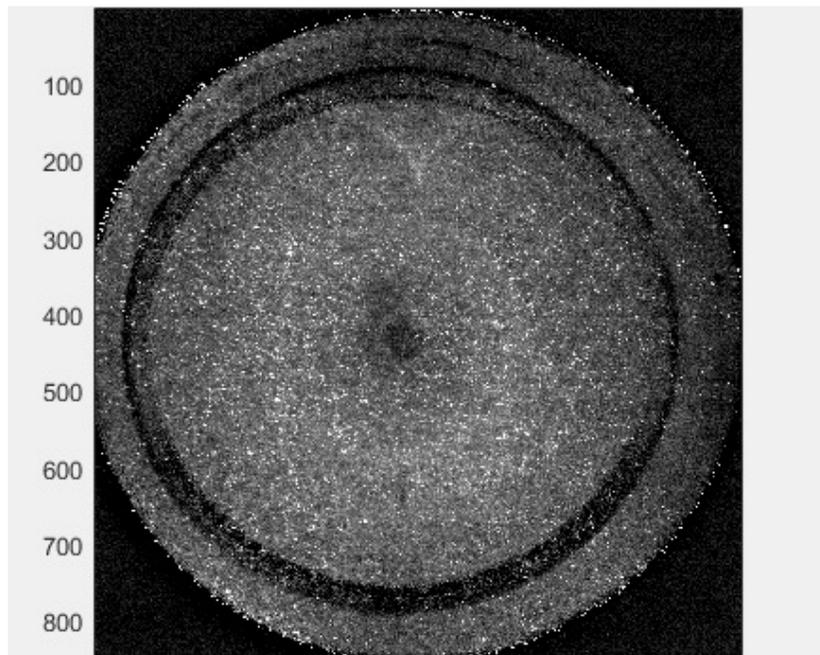
DMD growth  
rates

DMD  
amplitudes

## Experimental Configuration

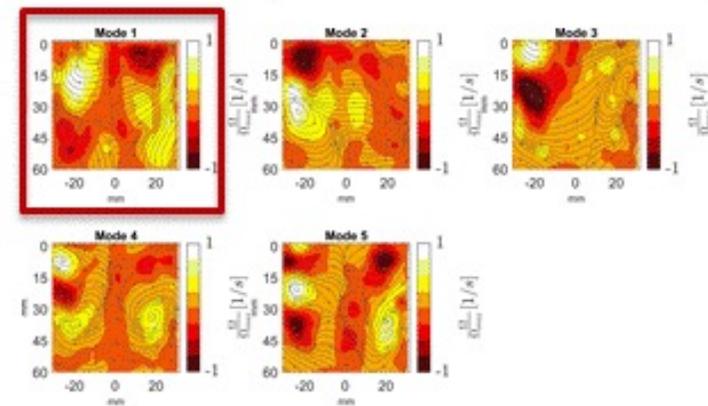
Isothermal flowfield dynamic coherent structures (PVC)

### Mie Signal

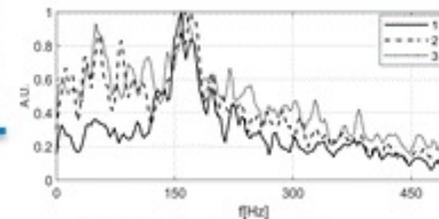


### POD Modes (Normalized Vorticity)

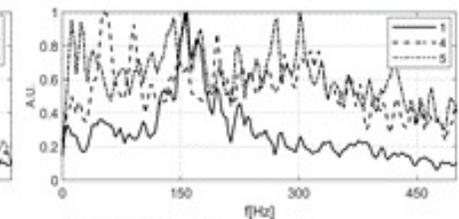
Wavemaker



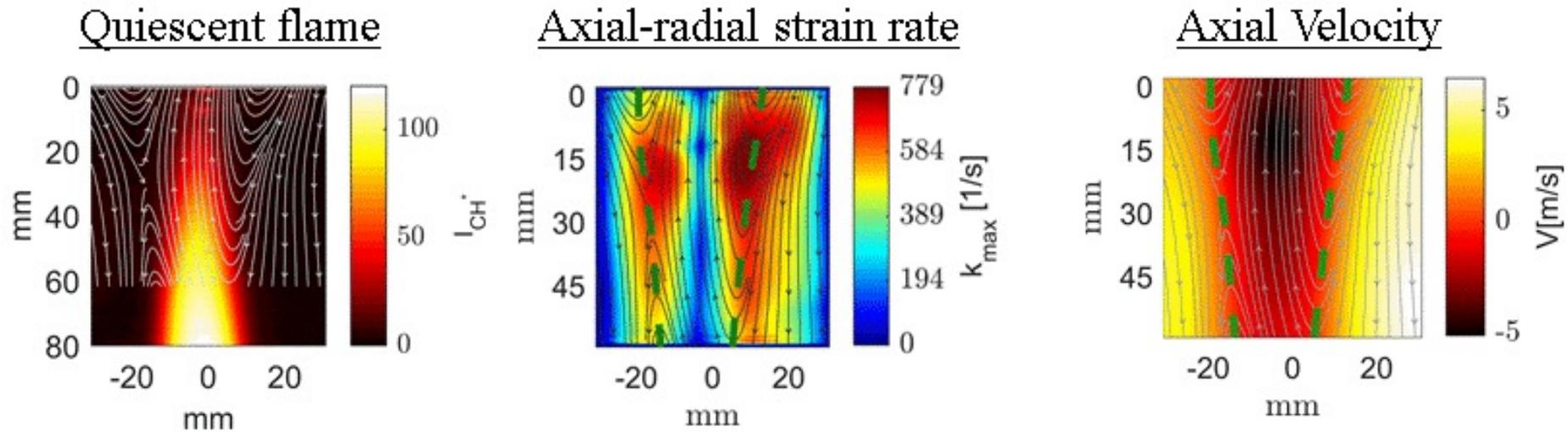
POD  
analysis



POD Spectra  
Modes 1,2,3

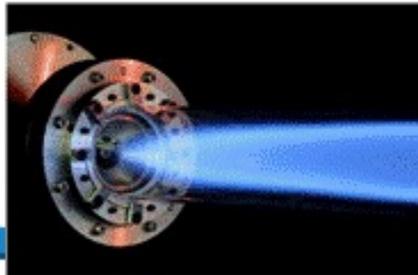


POD Spectra  
Modes 1,4,5



Long exposure image of a stable lean and elongated flame

- Flow structure similar to the isothermal.
- Flame anchoring within low strain rate regions



Flame and flowfield structure during triggering of intermittent thermoacoustic bursts

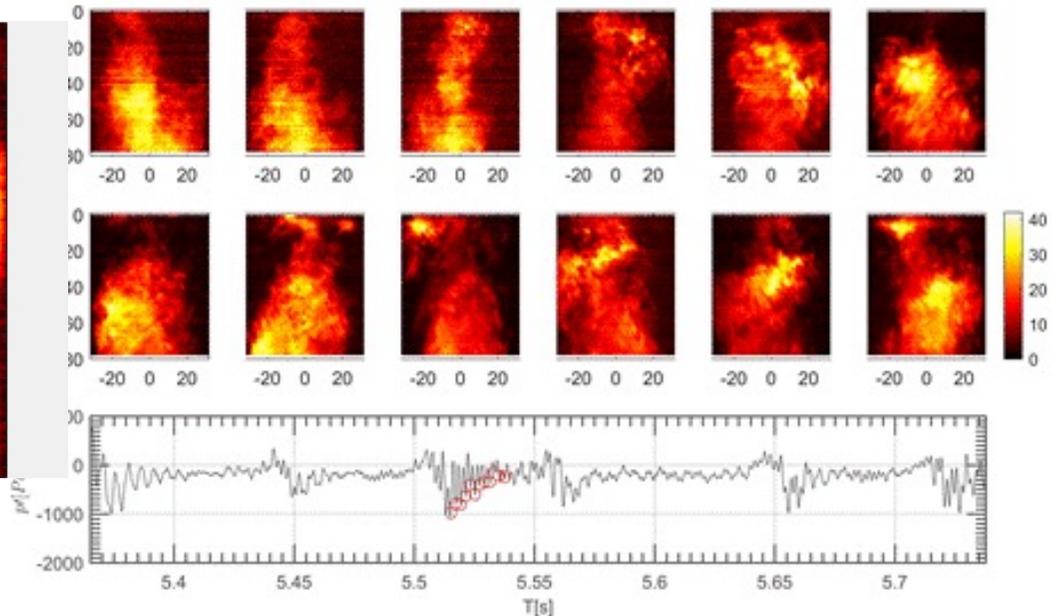
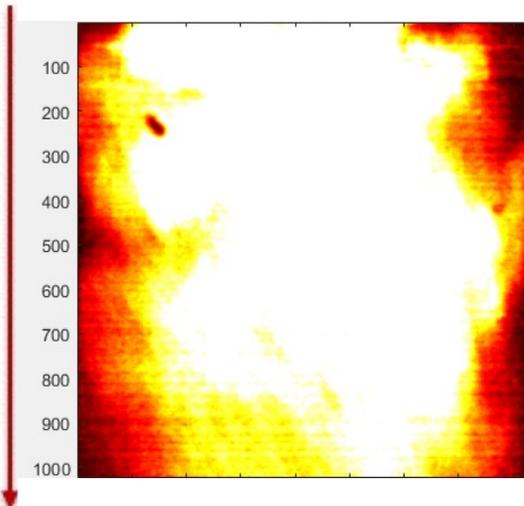
# Description of dynamic state transitions

Case D ( $\chi_{H_2}=0.30$ )

Instances of flame helical motion during thermoacoustic bursts

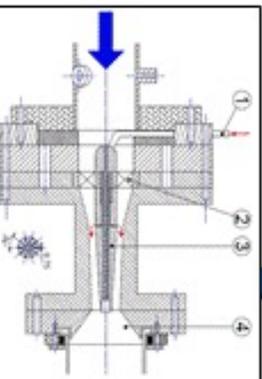
## Intermittent Flame Dynamics

Flow  
Direction



Dynamic pressure time series:

Note the red circles and corresponding snapshots

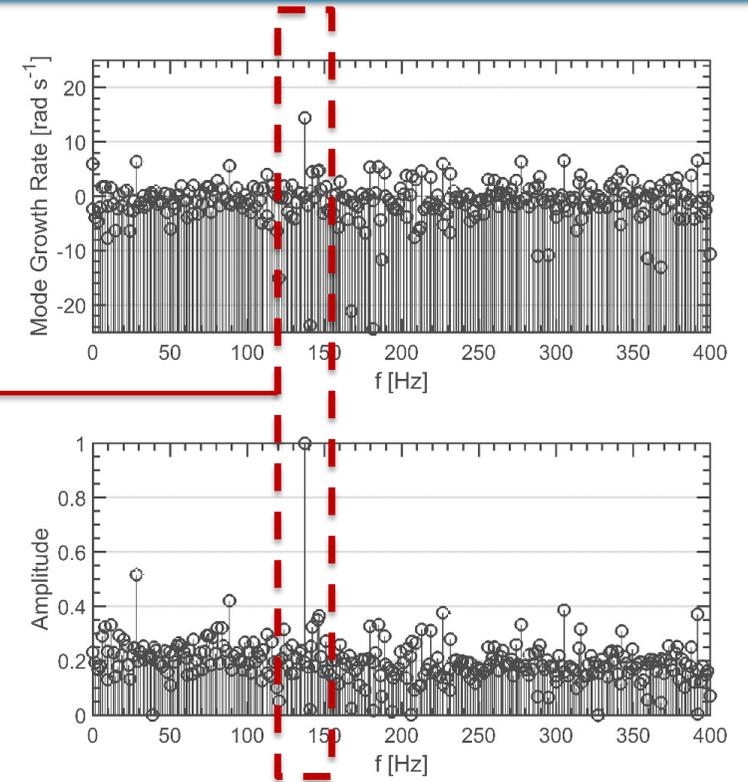
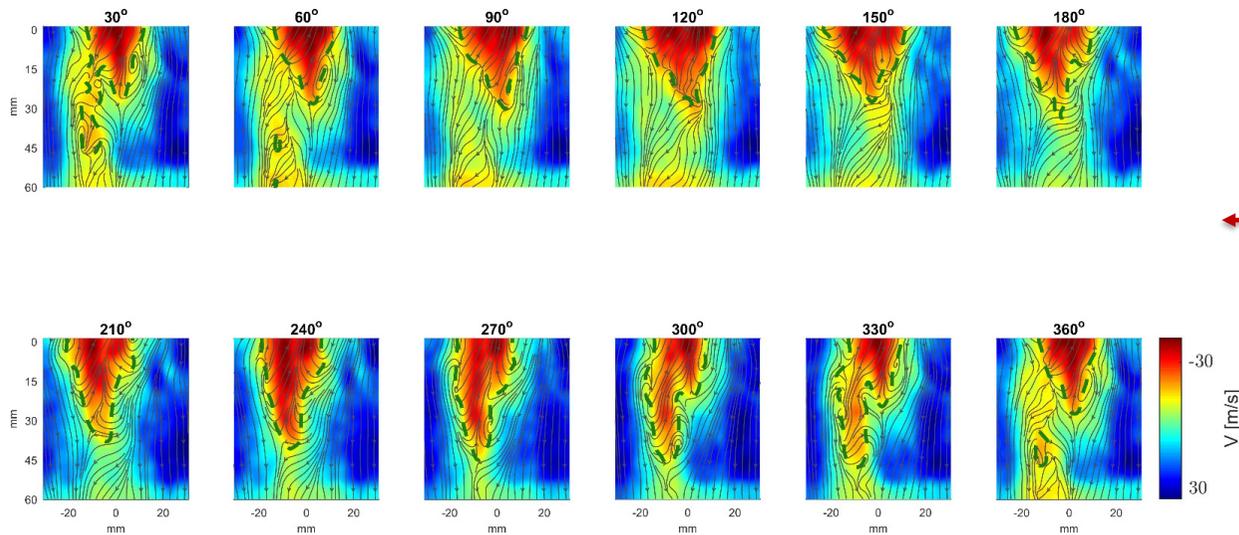


# Description of dynamic state transitions

Case D ( $\chi_{H_2}=0.30$ )

Precession as extracted via DMD

Filtering via DMD: Frequency of precession is very close to the isothermal PVC frequency of precession



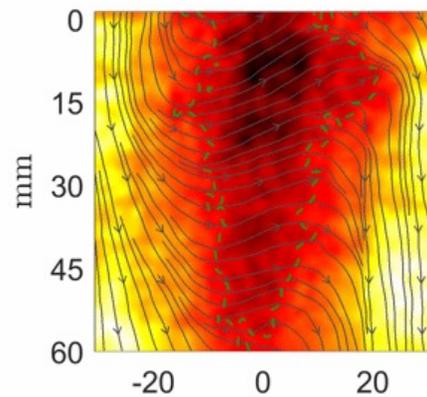
Frequency of precession: 137 Hz

# Description of dynamic state transitions

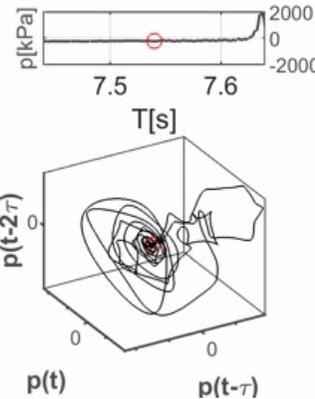
Case D ( $\chi_{H_2}=0.30$ )

Dynamic pressure phase space structure and intermittent flow dynamics

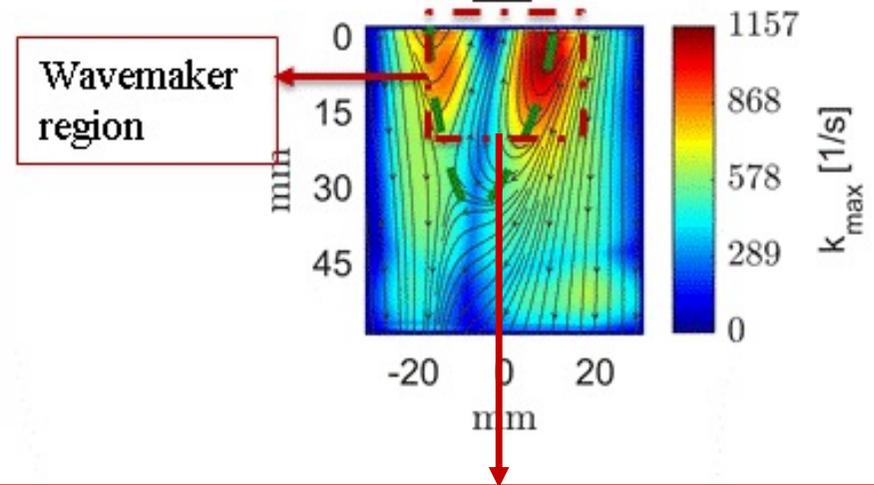
## Intermittent Flow Dynamics



Contours of axial velocity



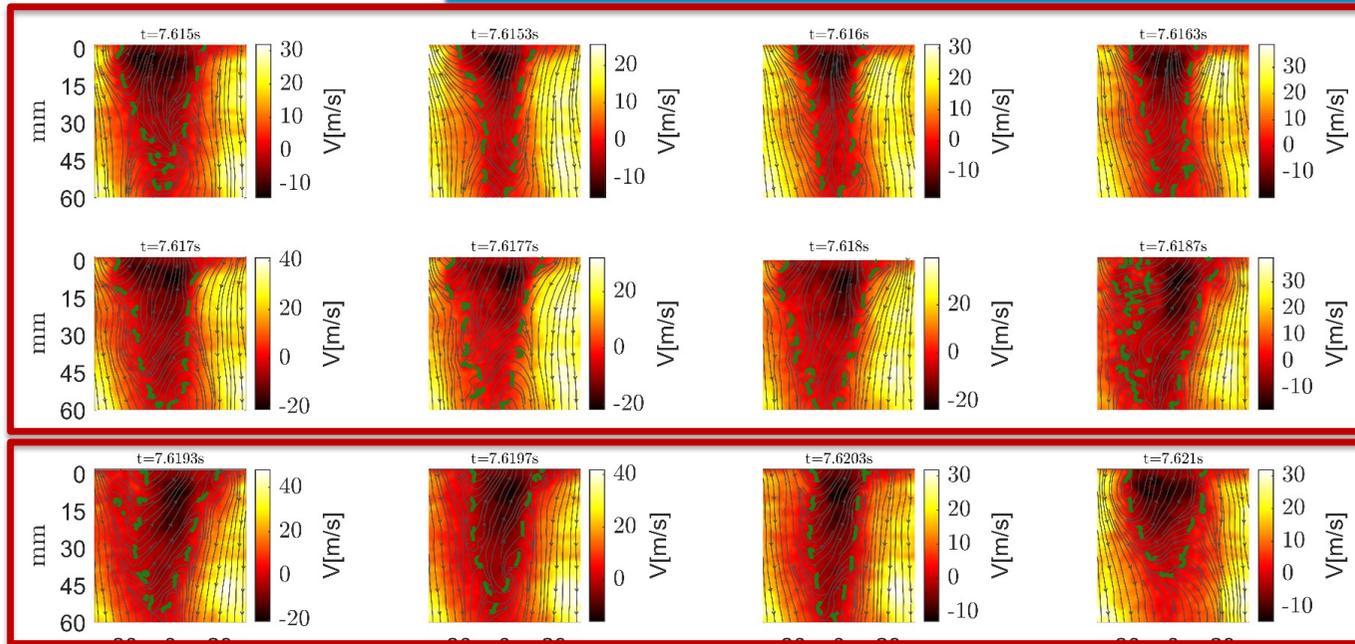
## Mean strain rate ( $k_{flow}$ ) during intermittency



If the elongated flame survives straining, such that it anchors close to the region wherein the helical wavemaker exists, then the flame precesses under the influence of the helical coherent structure (PVC)

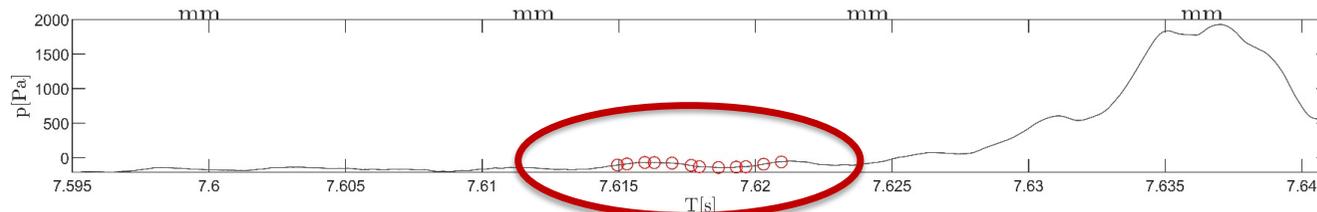
# Description of dynamic state transitions

## Breakdown of transition events: Pre-triggering



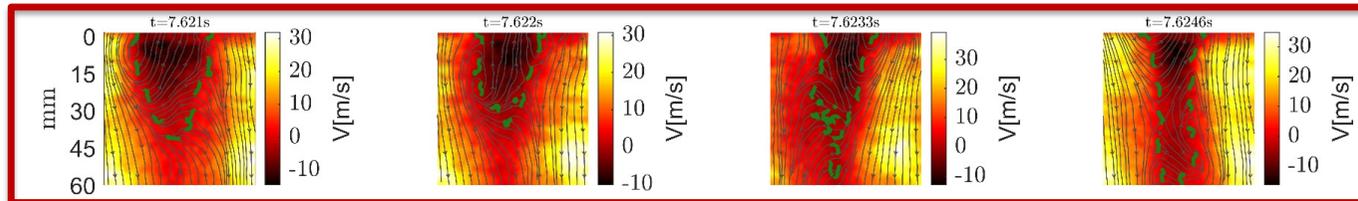
Initiation of helical motion of recirculation zone under the effect of helical coherent structures along the shear layers.

Initial formation of downstream axial stagnation point in the recirculation zone

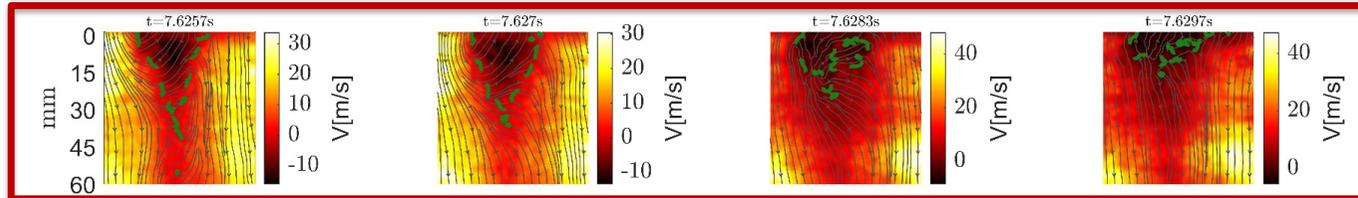


## Description of dynamic state transitions

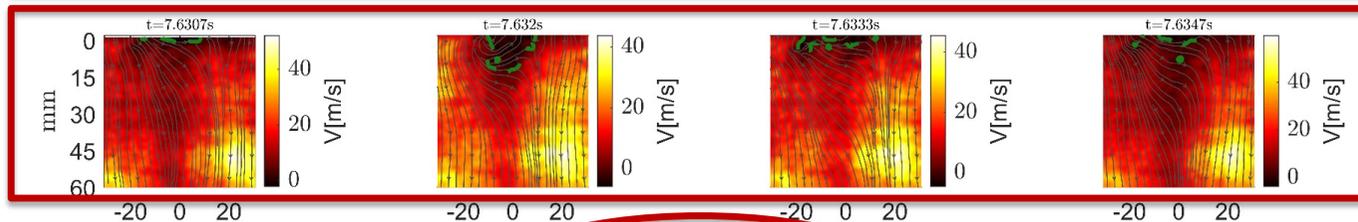
### Breakdown of transition events: Thermoacoustic burst



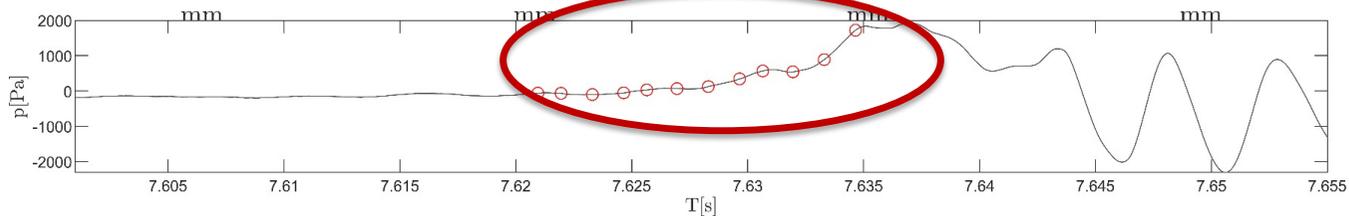
Convection of high axial velocity amplitude disturbance causing the recirculation zone to form a downstream axial stagnation point.



The downstream convection of the disturbance by the bulk flow decreases the axial and radial extent of the recirculation zone.

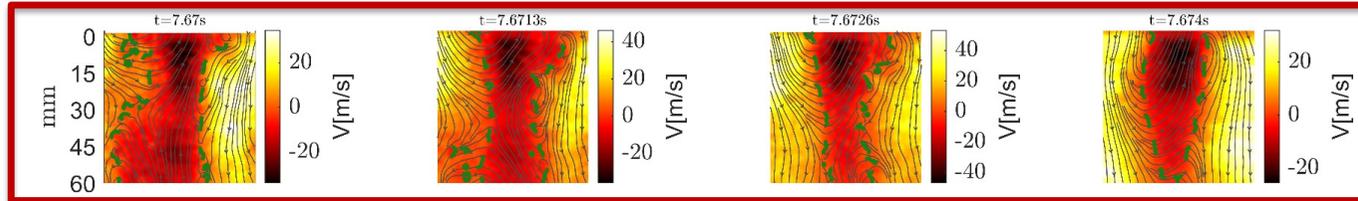


When the axial extent of the recirculation zone is minimum the dynamic pressure is maximum

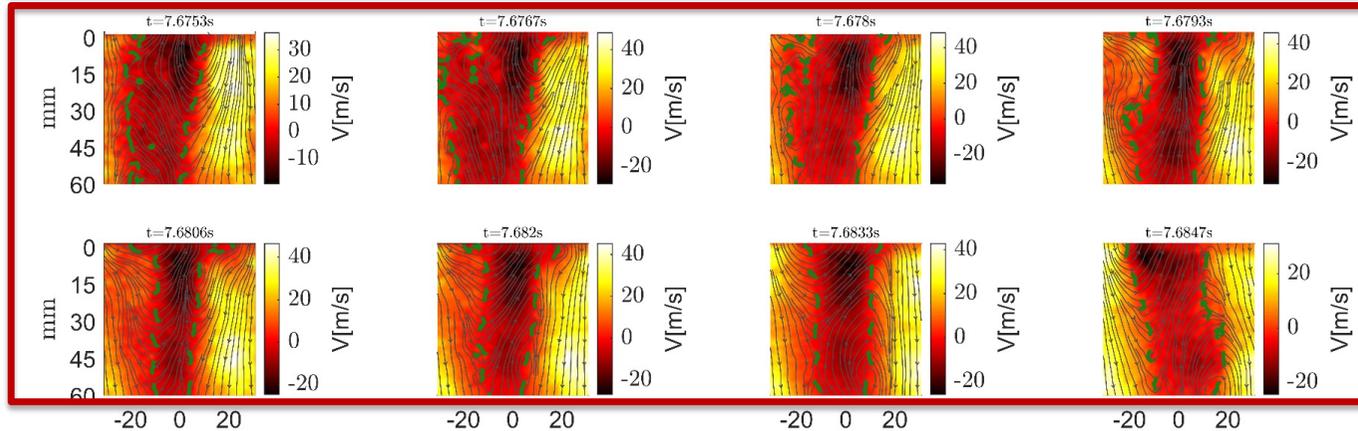


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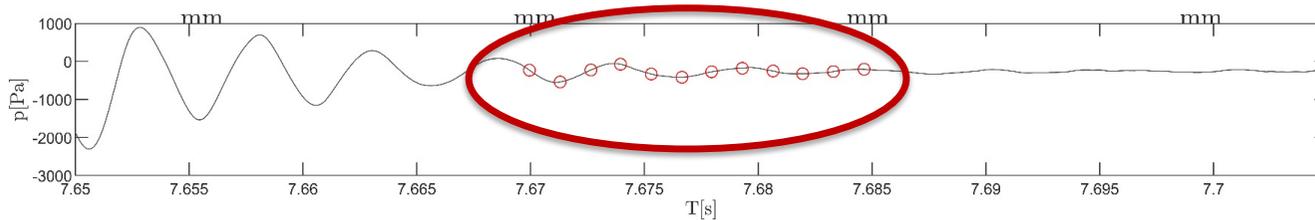
## Breakdown of transition events: Requiescence



Decreasing rate of helical precession



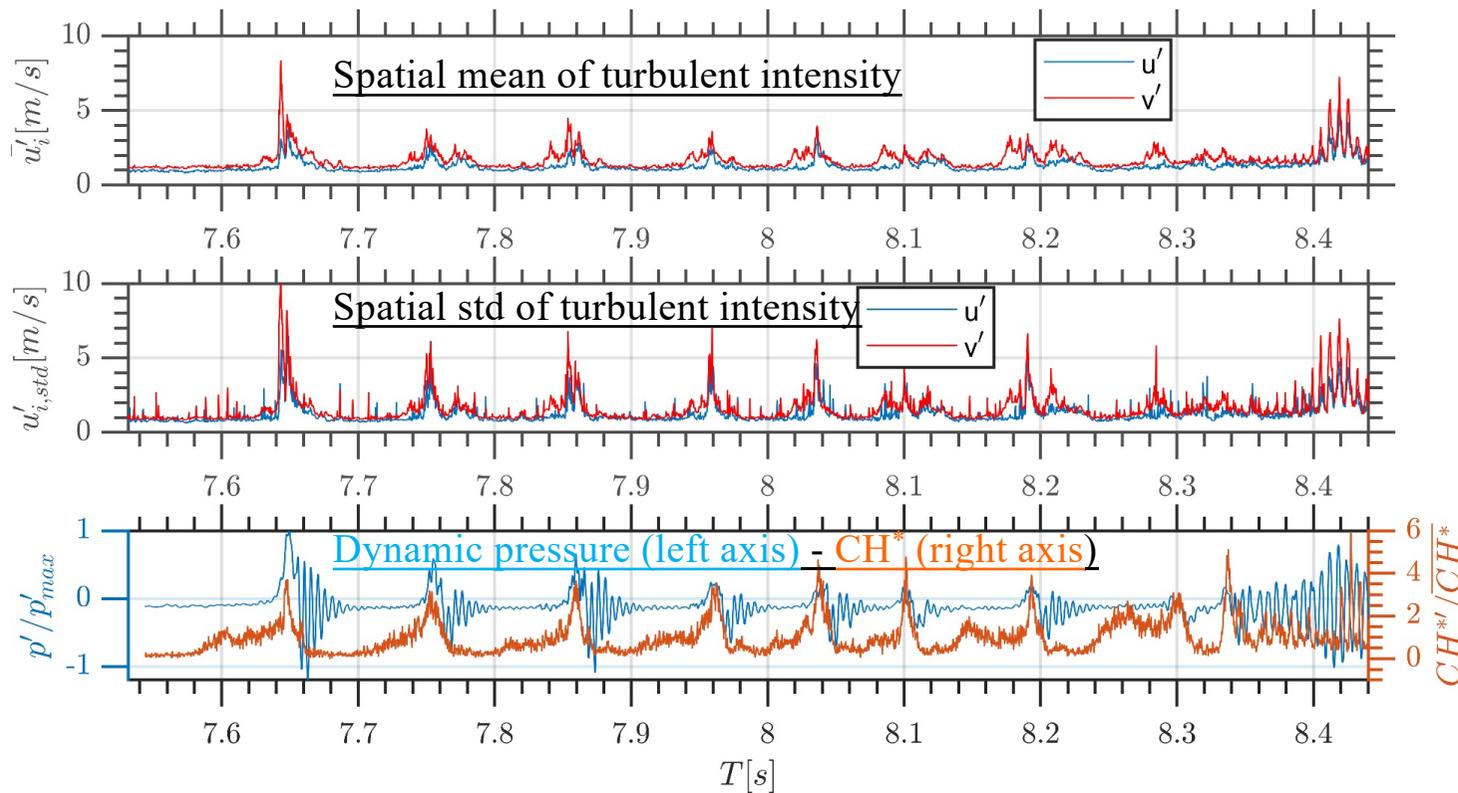
Reestablishment of open ended recirculation zone with no downstream stagnation point



# Description of dynamic state transitions

Case D ( $\chi_{H_2}=0.30$ )

Spatial mean and standard deviations of turbulent intensity

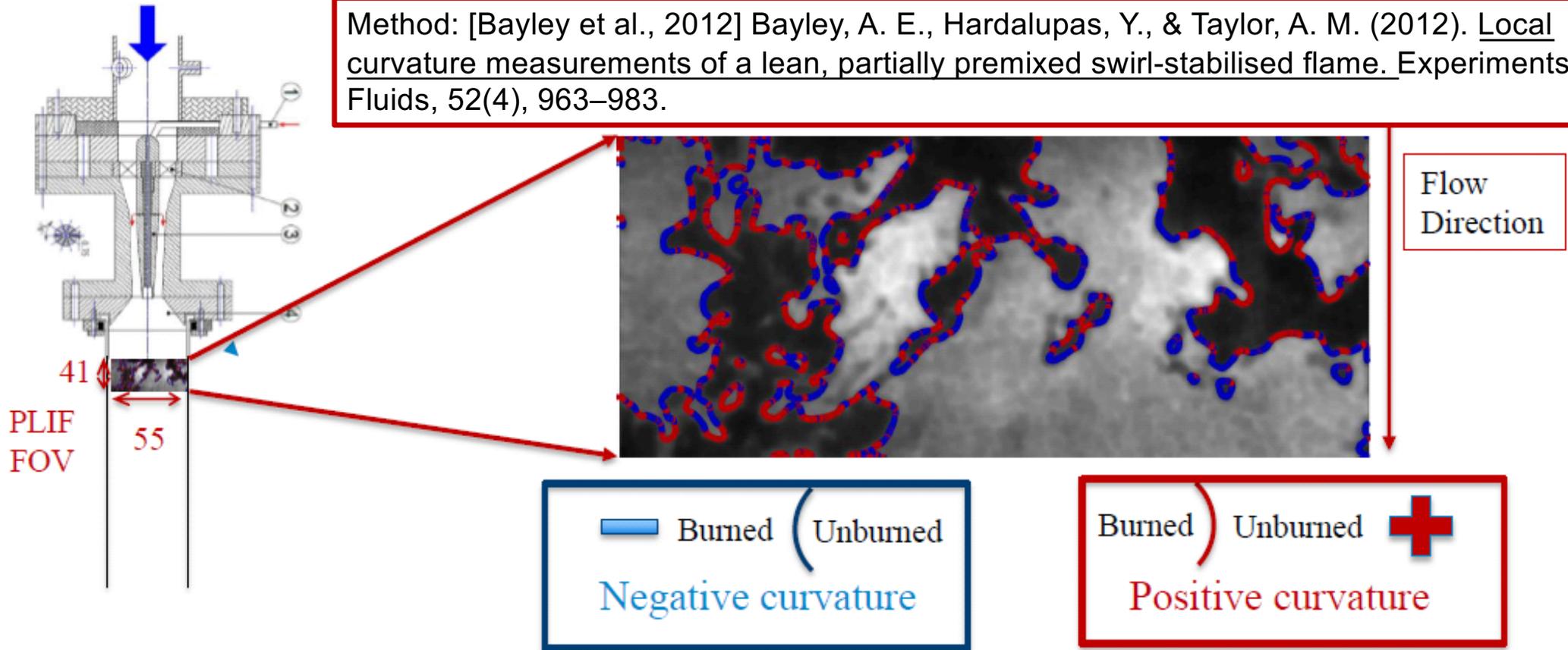


- The spatial mean and standard deviations of the turbulent intensities of the flowfield demonstrate spikes that coincide with the thermoacoustic bursts.
- The burning rate increases and the range of scales, with which the flame interacts, widens upon transitioning into thermoacoustic instability.

# Flame front curvature analysis

## Flame front detection algorithm

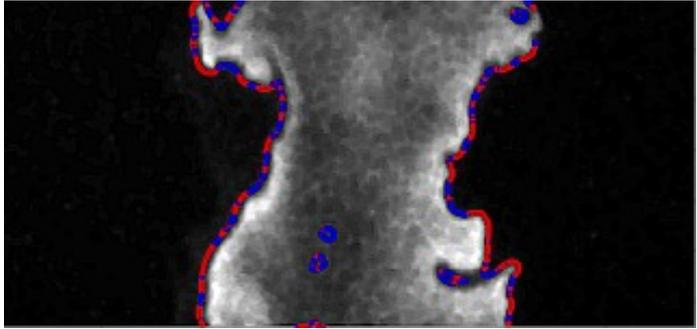
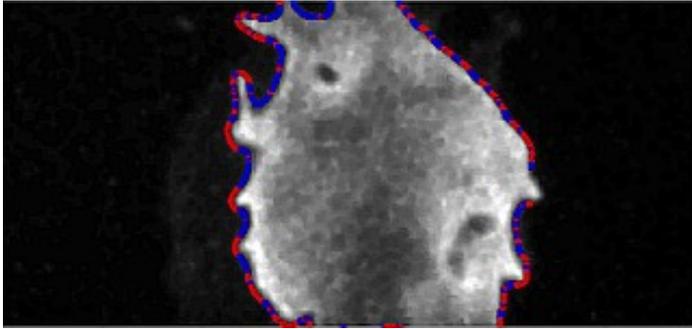
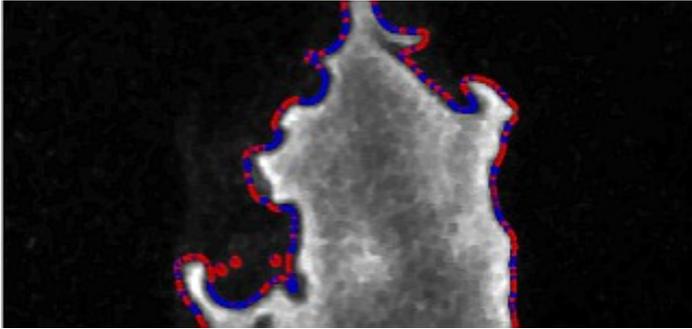
Method: [Bayley et al., 2012] Bayley, A. E., Hardalupas, Y., & Taylor, A. M. (2012). Local curvature measurements of a lean, partially premixed swirl-stabilised flame. *Experiments in Fluids*, 52(4), 963–983.



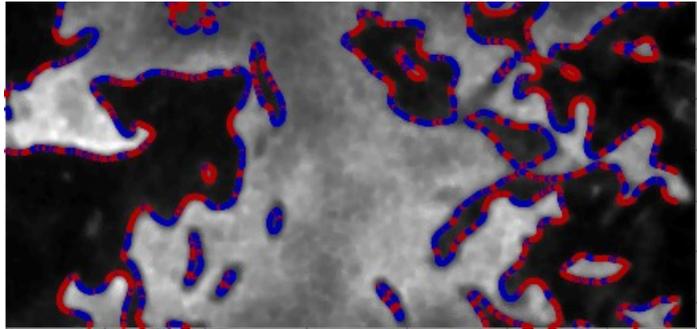
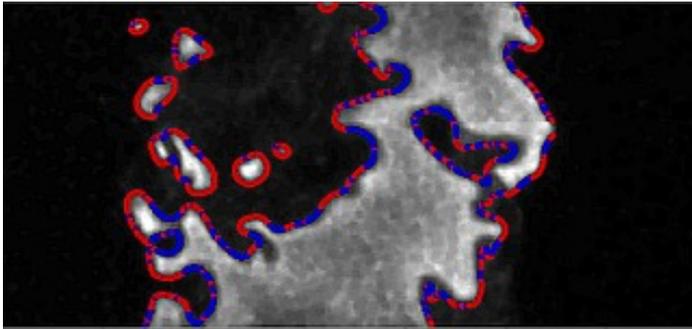
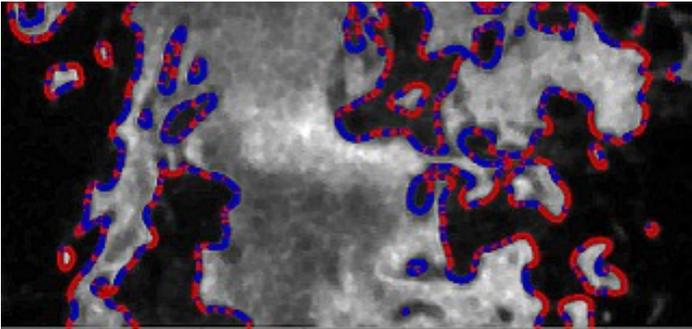
# Description of dynamic state transitions

Flame front curvature characteristics of intermittent flame via OH-PLIF measurements

Quiescent flames-straight and elongated.



Transitional flames-more wrinkled and with greater radial extent



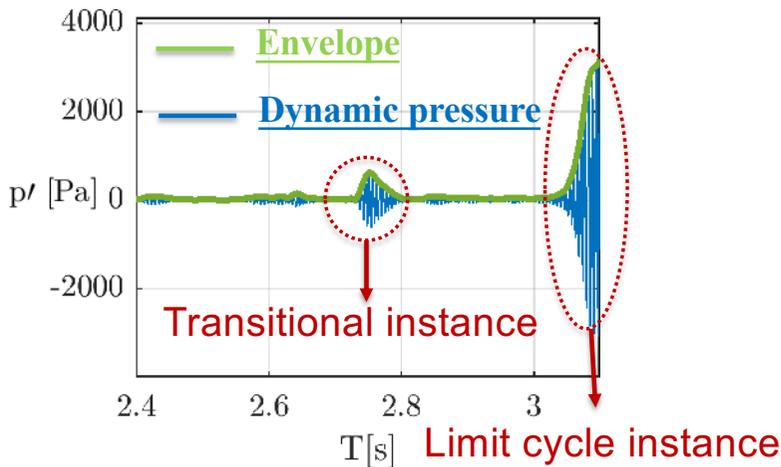
— Burned ( Unburned  
Negative curvature

Burned ) Unburned +  
Positive curvature

Reminder: Curvature convention

## Description of dynamic state transitions

Flame front curvature characteristics of intermittent flame via OH-PLIF measurements



Distinction between dynamic states:

Quiescent:  $p'_{\text{envelope}} < 300$  Pa

Transitional:  $p'_{\text{envelope}} > 300$  Pa for at most 20 thermoacoustic cycles

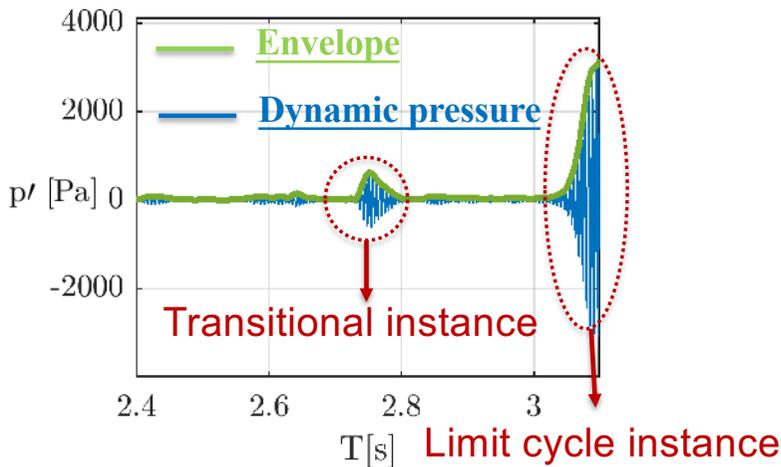
Limit cycle:  $p'_{\text{envelope}} > 300$  Pa for at least 20 thermoacoustic cycles

Case ID Thermoacoustic state	$\bar{\kappa}$ : Mean curvature	$\sigma$ : Standard deviation	$\mu_3$ : skewness	$\mu_4$ : kurtosis
D: Quiescent	0.115	1.108	0.091	5.045
D: Transitional	0.167	1.128	0.095	4.794
D: Limit Cycle	-0.036	1.416	-0.036	4.472
E : Quiescent	0.127	1.316	0.048	5.125
E: Transitional	0.087	1.330	0.047	4.755
E: Limit Cycle	-0.048	1.408	-0.031	4.577
F: Quiescent	0.122	1.264	0.027	5.344
F: Transitional	0.089	1.296	0.028	5.120
F: Limit Cycle	-0.024	1.402	-0.013	4.598

Upon transitioning from quiescence towards a limit cycle:  
Mean curvature decreases towards near zero negative values

## Description of dynamic state transitions

Flame front curvature characteristics of intermittent flame via OH-PLIF measurements



Distinction between dynamic states:

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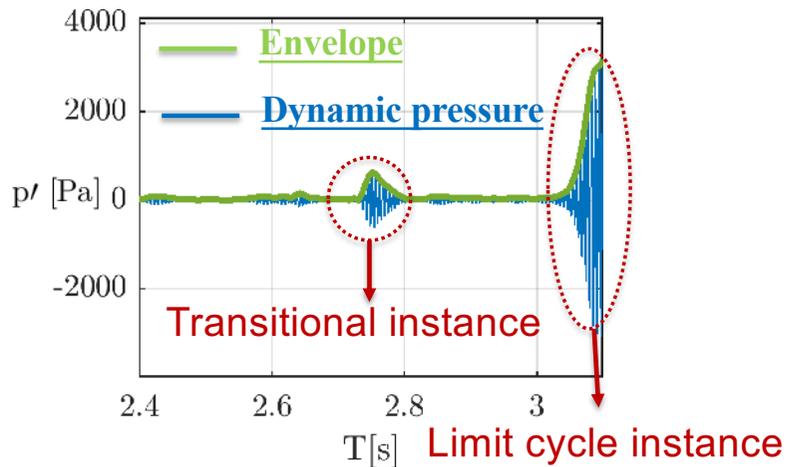
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Upon transitioning from quiescence towards a limit cycle:  
Standard deviation strongly increases.

## Description of dynamic state transitions

Flame front curvature characteristics of intermittent flame via OH-PLIF measurements



Distinction between dynamic states:

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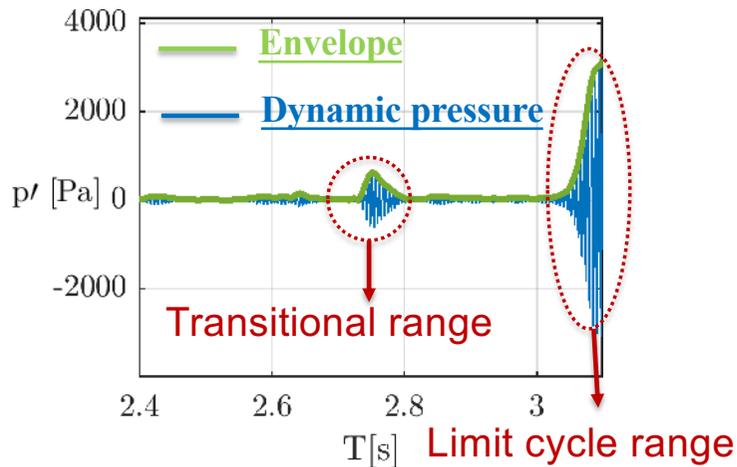
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Upon transitioning from quiescence towards a limit cycle:  
Standard deviation strongly increases.

Upon transitioning from quiescence towards a limit cycle:  
Kurtosis decreases

## Description of dynamic state transitions

Flame front curvature characteristics of intermittent flame via OH-PLIF measurements



Distinction between dynamic states:

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Flames that experience subcritical Hopf bifurcations gradually become more wrinkled while transitioning through the transitional thermoacoustic state towards the limit cycle.

## Summary 1/2: During a subcritical Hopf bifurcation, how does the flame and flowfield structure bifurcate?

- **Intermittency** is observed when the flame is able to penetrate into, and anchor at, the **“Wavemaker” region, close to the inlet of the burner**. To do so, the flame needs to overcome increased strain rates in this region of the flowfield.
- Flames **tolerant to extinction strain rates** are more susceptible to demonstrating subcritical Hopf bifurcations.
- Transition into instability in the model gas turbine combustor is associated with:
  1. **the PVC** which imposes **helical** disturbances on the flame and the recirculation zone.
  2. **Loss of randomness** in the dynamic state: can be employed to forewarn of triggering.
- The role of the **PVC** is **crucial**. It exists **both** for the **isothermal** and the **quiescent** flowfields and it can instigate (“kick the system”) thermoacoustic bursts that are promoted mainly by the flame-wall interactions.

Summary 2/2: During a subcritical Hopf bifurcation, how does the flame and flowfield structure bifurcate?

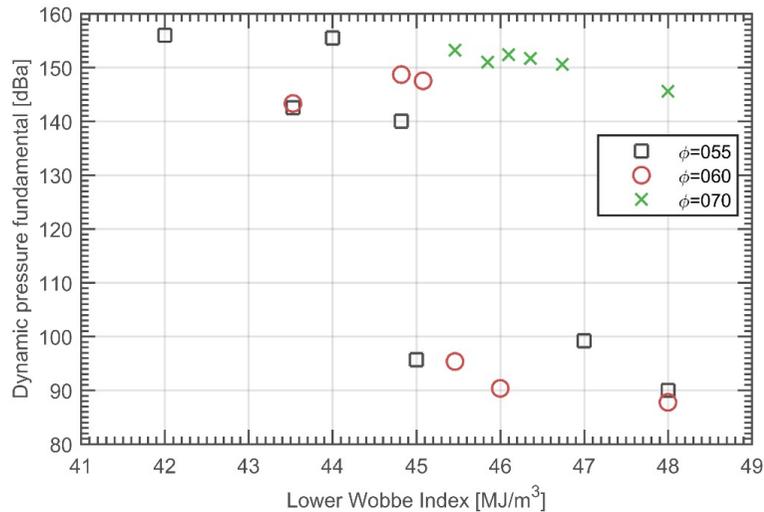
- The **flames** of thermoacoustic systems demonstrating intermittency assume increasingly **wrinkled** forms. This is supported by both PIV and PLIF measurements:
  1. The standard deviation of the **turbulent intensities** during the transition into thermoacoustic instability increases.
  2. The standard deviation and the kurtosis of the **flame front curvature** increase.

## Summary 2/2: During a subcritical Hopf bifurcation, how does the flame and flowfield structure bifurcate?

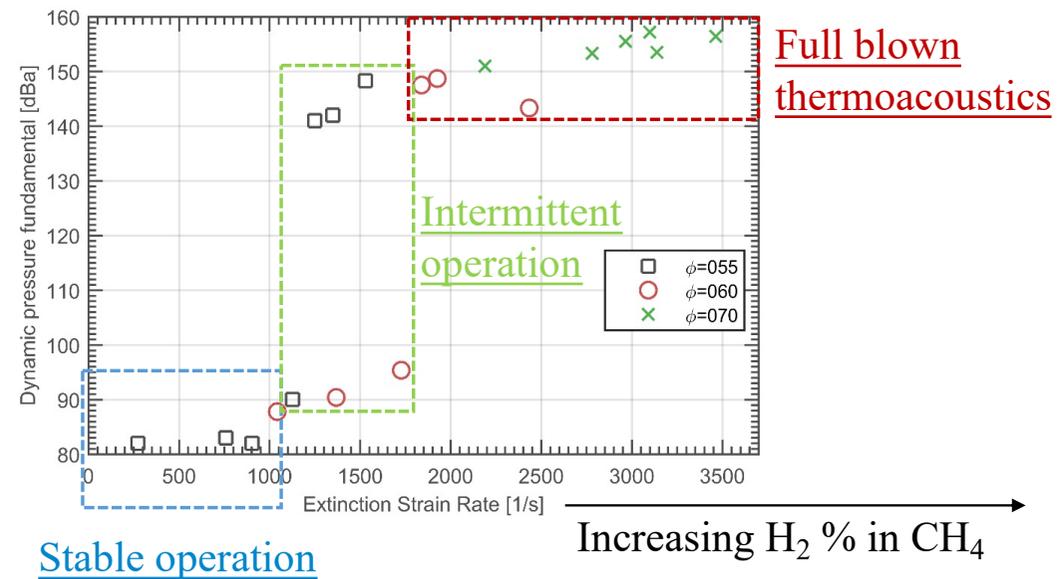
- Note that we have made no mention of
  - any acoustic frequency, Because the limit cycle has not been established yet in order to make a case about harmonics and subharmonics
  - a PVC (settles at the subharmonic) because its emergence is dependent on the limit cycle phase.
    - The PVC is suppressed when the flame moves back into the centerbody and detaches from its downstream half due to the strain rate. The PVC on the limit cycle, and has also been corroborated in the literature, appears at a natural frequency of 255 Hz- during the limit cycle - and gives a distinct heat release rate contribution at 85Hz - the subharmonic. It is the difference between  $f_{pvc}$  and the fundamental of the acoustics.

# Motivation: Extinction strain rate is a mixture property collapsing dynamic state transitions (H<sub>2</sub> enriched CH<sub>4</sub> blends)

Collapsing dynamics with Wobbe index



Collapsing dynamics with extinction strain rate



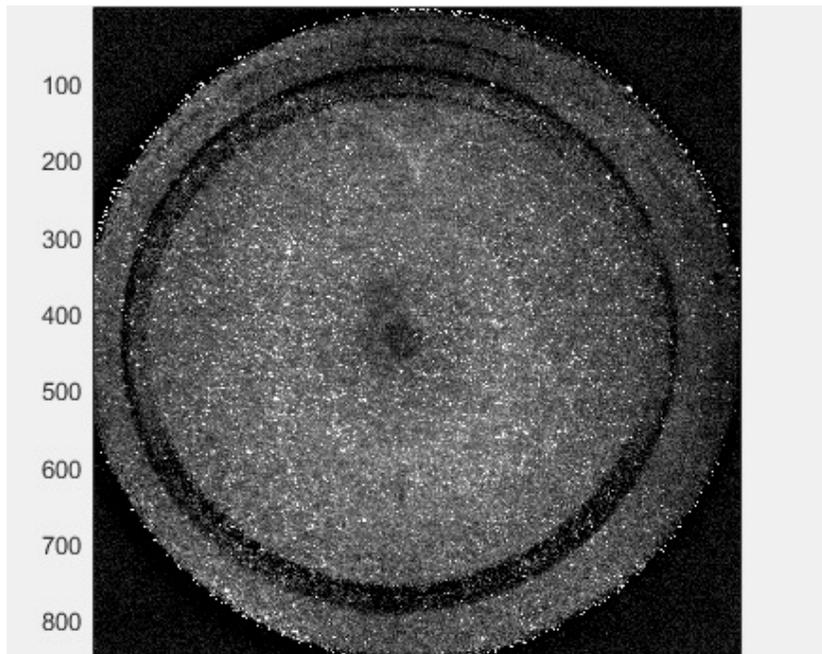
Karlis, E., Liu, Y. Hardalupas, Y., & Taylor, A. M. (2019d) H<sub>2</sub> enrichment of CH<sub>4</sub> blends in lean premixed gas turbine combustion: An experimental study on effects on flame shape and thermoacoustic oscillations dynamics. *Fuel*, 254, 115524

Supportive slides

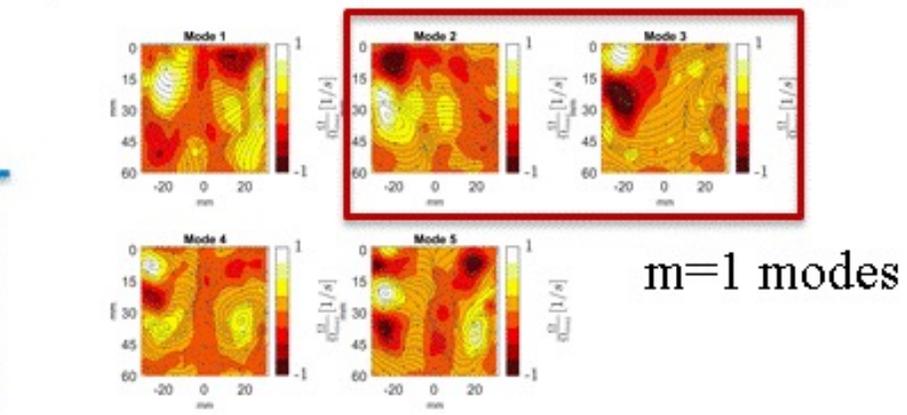
# Experimental Configuration

Isothermal flowfield dynamic coherent structures (PVC)

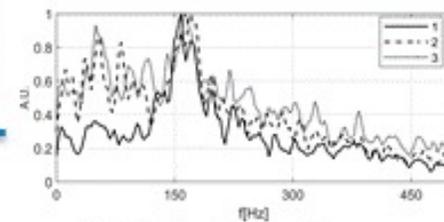
Mie Signal



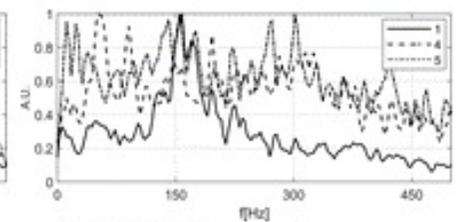
POD Modes (Normalized Vorticity)



POD  
analysis

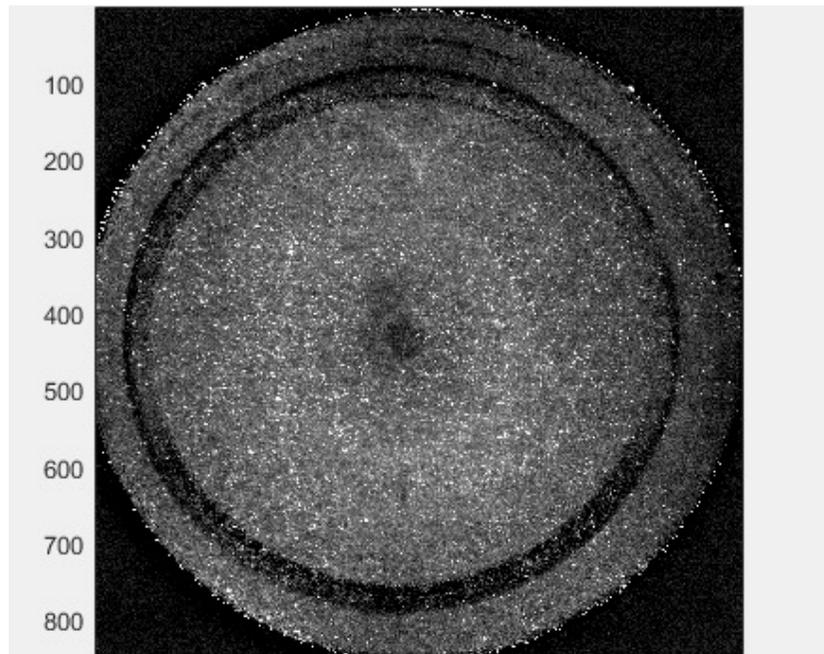


POD Spectra  
Modes 1,2,3

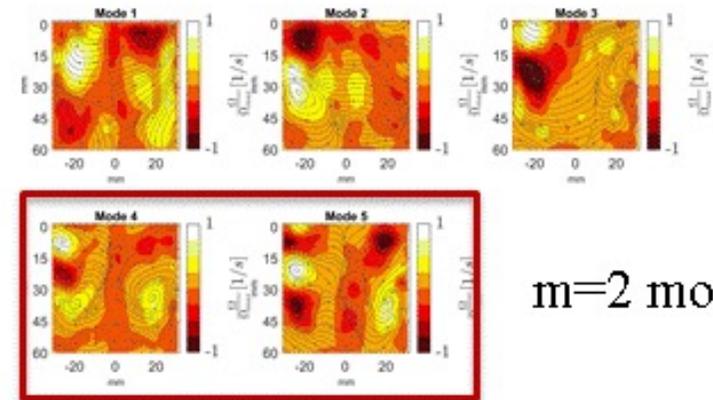


POD Spectra  
Modes 1,4,5

Mie Signal

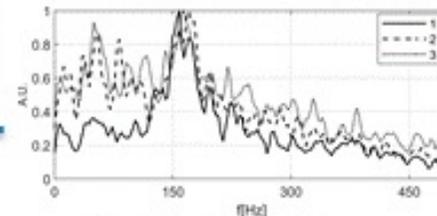


POD Modes (Normalized Vorticity)

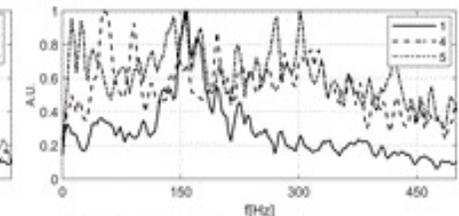


m=2 modes

POD  
analysis



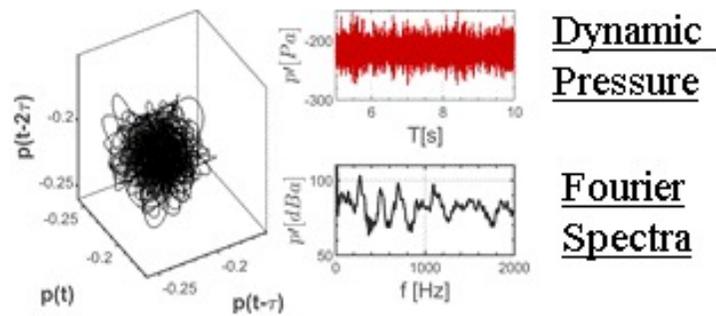
POD Spectra  
Modes 1,2,3



POD Spectra  
Modes 1,4,5

Intermittency: Interpretation of transitional dynamics  
Phase space representation

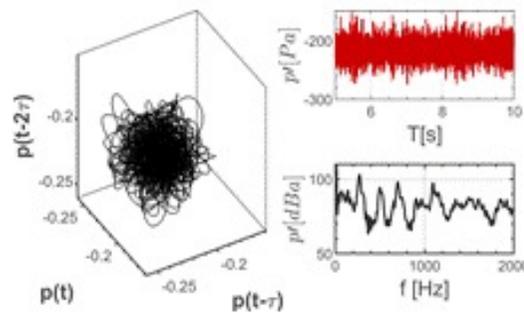
Quiescence



Cases B, C

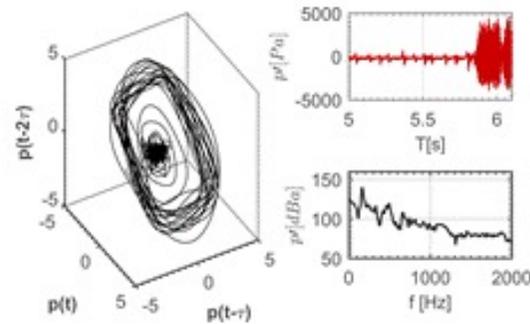
Dynamics: Attracted to fixed point and demonstrate stochastic low amplitude pressure fluctuations.

Quiescence



Cases B, C

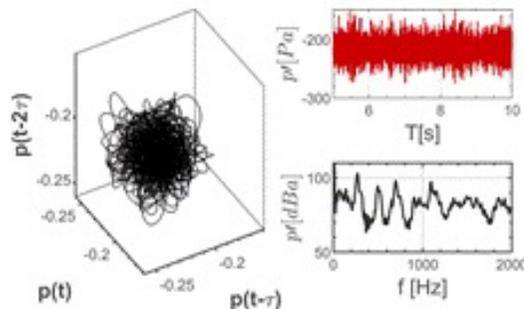
Intermittency



Case D

Dynamics: Toroidal transition between limit cycle and fixed point. Emergence of coherent dynamics amidst a quiescent background.

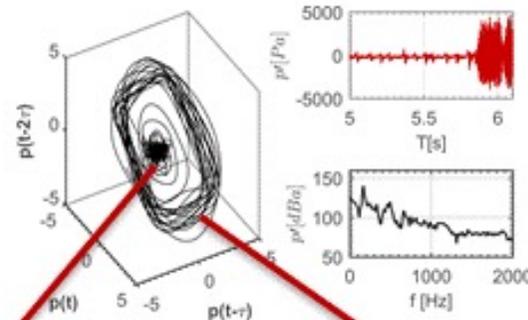
Quiescence



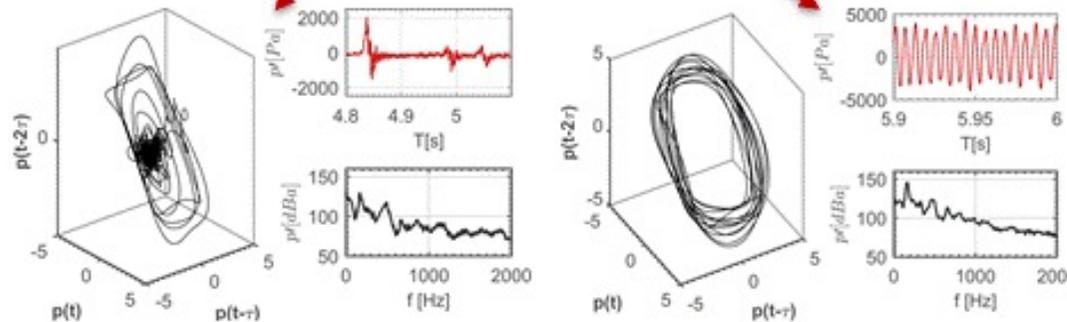
Cases B, C

Dynamics: Fixed point and toroidal transition

Intermittency

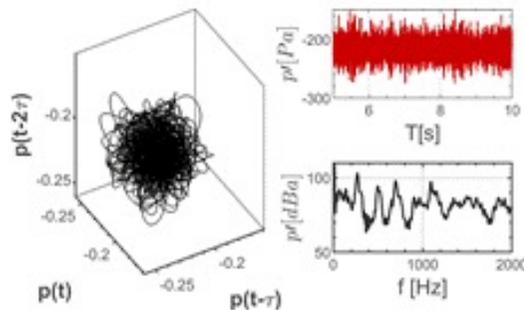


Case D



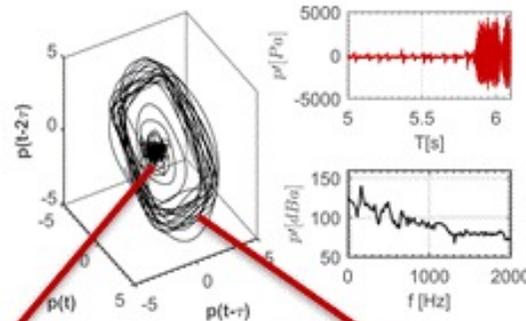
Dynamics: Limit cycle

Quiescence



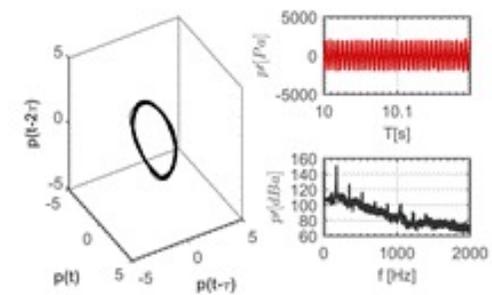
Cases B, C

Intermittency



Case D

Limit Cycle



Case G

Dynamics:  
Consistent attraction  
to limit cycle.

